

Course Outline (TPG 565: Quantum Mechanics (4 credits))

1. Fundamental Concepts:

Review of linear algebra, Postulates, Observables, Measurements, Ehrenfest theorem, Uncertainty principle, Density matrix.

2. Quantum Dynamics:

Schrödinger picture, Heisenberg picture, Dirac/Interaction picture, Dyson series, Conservation of probability.

3. Harmonic Oscillator:

Dirac operator method, Uncertainty of energy eigenstates, Time evolution of ladder operators, Coherent states.

4. Symmetry:

Symmetry in classical physics, Review of group theory, Lie groups, Lie algebras and their representations, Symmetry in quantum mechanics, Discrete and continuous symmetries.

5. Theory of Angular Momentum:

Rotations and angular momentum, $SO(3)$, $SU(2)$ and Euler rotations, Spin-1/2 and spin-1 systems, Addition of angular momentum, Clebsch–Gordan coefficients.

6. Approximation Methods:

Time independent perturbation method: Non-degenerate and Degenerate Cases, Variational method, WKB Method, Time dependent perturbation theory.

7. Scattering:

Scattering amplitude, Partial wave analysis, Born approximation, Optical theorem, Lippmann-Schwinger equation and its formal solution.

8. Relativistic Quantum Mechanics:

Klein-Gordon equation, Dirac equation.

9. Identical Particles:

Bosons and fermions, Spin-Statistics theorem, Non-Standard statistics, Anyonic Statistics, Parastatistics.

10. Miscellaneous Topics:

Quantum Entanglement, Entanglement entropy, EPR Paradox, Bell's theorem.

References Books:

1. J. J. Sakurai, Jim Napolitano, Modern Quantum Mechanics.
2. Ramamurti Shankar, Principles of Quantum Mechanics.
3. Horatiu Nastase, Quantum Mechanics: A Graduate Course.