

INSTITUTE OF STATISTICAL RESEARCH AND TRAINING  
UNIVERSITY OF DHAKA

CURRICULUM AND SYLLABUS

B.S. Honours Program in APPLIED STATISTICS AND DATA SCIENCE

Session: 2022–2023

[www.isrt.ac.bd/academics/undergraduate](http://www.isrt.ac.bd/academics/undergraduate)

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# 1 Institute of Statistical Research and Training

## 1.1 Introduction

The Institute of Statistical Research and Training (ISRT), University of Dhaka, is the leading institution for training and research in Applied Statistics and Data Science in Bangladesh. It was founded in 1964 by the Late National Professor Dr. Qazi Motahar Husain, an eminent scientist, academician, and a leading proponent of the statistical sciences in this country. The Institute offers a 4-year B.S. Honours program designed to produce graduates with strong statistical computing skills, sound knowledge of statistical concepts, and the versatility to apply these concepts in areas as diverse as medicine, engineering, business, economics, and the social sciences. The 1-year M.S. program consists of specialized courses in areas ranging from environmental statistics to statistical signal processing, statistical machine learning, and causal inference and has been designed for students with a keen interest in higher studies and research. In addition, the Institute offers Ph.D. and M.Phil. degree programs. Highly experienced faculty members, most of whom have Ph.D. degrees from reputed universities across the world, run these programs.

ISRT boasts an academic environment that is highly competitive and conducive to research. Both students and faculty members benefit from the regular seminars and talks given by researchers from home and abroad on topics of current interest. The Institute has a rich library with well over 15,000 books. It has three state-of-the-art computer labs, cloud computing facilities, and high-speed internet access for graduate and undergraduate students. The aim is to provide a learning environment that stimulates intellectual curiosity, critical thinking, and independent problem-solving skills. The Journal of Statistical Research (JSR), an international journal published bi-annually by ISRT since 1970, is a forum for exchanging research ideas between statisticians in Bangladesh and abroad. Faculty members have research interests in diverse areas such as biostatistics, machine learning, spatial statistics, statistical pattern recognition, public health, Bayesian analysis, and econometrics. They regularly disseminate their research works in peer-reviewed journals and international conferences.

Among its other activities, the Institute frequently organizes short courses and training programs for non-statisticians working in government and non-government organizations who need statistical analysis. In doing so, it has played an active role in promoting and creating awareness about the need for sound statistical practices among people from other disciplines so that they may work more efficiently within their organizations. ISRT also maintains close ties with the Bangladesh Bureau of Statistics (BBS) and other organizations responsible for

collecting and disseminating statistical data in Bangladesh. It is frequently called upon to offer its expertise on statistical issues of national interest. Over the years, the Institute has played a significant role in the country's development by producing world-class statisticians for academia and industry and providing statistical expertise on issues of national interest. In addition, the Institute provides statistical consulting services through StatLab primarily for the students and faculty members of the University of Dhaka, aiming to strengthen research on campus by assisting graduate students and faculty members of other disciplines.

## 1.2 Vision and Mission of the Institute

### Vision

The vision of the Institute is to take a leading position globally in providing quality education in Applied Statistics and Data Science, conducting leading-edge research, and creating innovative industrial partnerships.

### Mission

The Institute's mission is to produce competent graduates in Applied Statistics and Data Science equipped with the skills necessary for success in a technological society and competitive global environment who will fulfill the statistical demands of the nation and the world.

### Objectives

To fulfil the vision and missions, ISRT aims to

- (i) Strengthen and update various teaching and training programs at undergraduate, post-graduate, and doctoral levels to produce graduates with strong theoretical and practical knowledge of statistical science in line with the labor market requirements.
- (ii) Create an environment conducive to high quality research.
- (iii) Contribute to advancing science and technology through interdisciplinary research, jointly with scientists, scholars at the University of Dhaka, and other research institutions at home and abroad.
- (iv) Contribute to the statistics profession and the larger scientific community by running quality statistical journals and serving on editorial boards, review panels, and administrative and advisory committees.
- (v) Employ high quality faculty members with diverse research interests.
- (vi) Promote the exchange of knowledge and ideas by arranging invited talks regularly in addition to workshops and international conferences.
- (vii) Disseminate statistical knowledge by offering training programs to students of other departments and professionals of various government and private organizations.
- (viii) Serve the University's and national bodies' statistical needs by providing consulting services in research, government, business, and industry.
- (ix) Produce graduates having strong moral and ethical values, respect for local norms and culture, and exceptional leadership qualities.

# 2 B.S. Honours Program in Applied Statistics and Data Science

## 2.1 Introduction

The B.S. honours program in Applied Statistics and Data Science is an integrated four-year program. A student with high academic attainment in Secondary School Certificate (S.S.C.) and Higher Secondary School Certificate (H.S.C.) or equivalent levels with Mathematics as a subject of study is eligible for admission. Unless otherwise stated, the regulations for admission of the students and the examinations will be the same as those for the B.S. honours courses in the Faculty of Science. The program includes theoretical and applied courses with intensive computing facilities. However, the program emphasizes applying statistical techniques to real-life problems arising in medicine, engineering, business and social, environmental, and biological sciences. The course is so designed that graduates are equipped to work efficiently and competently in government and non-government organizations, research organizations, service departments, and other related fields after successful completion.

## 2.2 Structure of the Program

The 4-year B.S. Honours program comprising of four academic sessions, each having a duration of 12 months. Each student has to take a total of 140 credits over four academic years. These include 105 credits of theoretical courses, 24 credits of computing courses, eight credits of oral, and three credits for a Capstone project. Out of 140 credits, 30 will be from Mathematics, Economics, and Computer Science courses. In addition, the student has to take a non-credit course on English communication skills in the first academic year. Detail breakdown of the distribution of the courses with credit hours is given in Section 2.4.

Table 2.1: Distribution of 12 calendar months by different components of the program

Type	Duration (in weeks)
Classes	26
Preparation of final examination	4
Course final examination	6
Result publication	4
Vacations and holidays	12

The credit is defined differently for theoretical and computing courses. For theoretical courses, one credit corresponds to 15 class hours, where each class is of 50 minutes. For computing courses, one credit corresponds to 15 class hours of 50 minutes each for lab work and 15 hours for practice. Non-credit courses consist of 20 classes, each of which is 1.5 hours.

## 2.3 Assessment System

### 2.3.1 Evaluation

A student's performance at each year in a given course will be evaluated by in-course examinations/assignments/performance evaluation in the class/final examinations. Evaluations are aggregated at the end of each academic year. Thirty percent marks of the theoretical and forty percent of the computing courses will be allotted for in-course examinations and attendance.

There will be two in-course examinations for each theoretical, computing, and non-credit course. The course teacher may decide to use short questions to evaluate students in in-course examinations. Each in-course assessment will be of one-hour duration for a theory course and the non-credit course, and the average of marks from two exams will be the final mark. However, an in-course assessment will be 1.5 hours for a computing course, and the sum of two marks will be the final mark. The theoretical course final examinations will be 4 hours for 4-credit courses and 3 hours for 3-credit courses. The duration of practical courses' final examinations will be of 4 hours.

Table 2.2: Marks (%) allocation for theoretical, computing, and non-credit courses

Theoretical	Attendance	05
	In-course exam	25
	Final exam	70
Computing	Attendance/assignment	10
	In-course exam	30
	Final exam	60
Non-credit	Attendance	10
	In-course exam	25
	Quizzes (5 or 6), assignments, presentations and/or mini projects	65

*The performance in the non-credit course will be considered as either Satisfactory or Non-satisfactory based on the cut off point of 40 out of 100*

Table 2.3: Marks distribution for attendance

Attendance (%)	Marks (%)
90 and above	5
85 to 89	4
80 to 84	3
75 to 79	2
60 to 74	1
< 60	0

### 2.3.2 Grading and Grade Point

Grades and grade points will be awarded on the basis of marks obtained in the written, oral and practical examinations.

Table 2.4: Percentage score, letter grade, and grade points

Marks Obtained (%)	Grade	Grade Point
80–100	<i>A+</i>	4.00
75–79	<i>A</i>	3.75
70–74	<i>A–</i>	3.50
65–69	<i>B+</i>	3.25
60–64	<i>B</i>	3.00
55–59	<i>B–</i>	2.75
50–54	<i>C+</i>	2.50
45–49	<i>C</i>	2.25
40–44	<i>D</i>	2.00
< 40	<i>F</i>	0.00
	<i>I</i>	Incomplete
	<i>W</i>	Withdrawn

Only “D” or higher grades will be counted as credits earned by a student. Grade point average (GPA) will be calculated as the weighted average of the grade points obtained by a student in all the courses completed in a year. GPA will be calculated according to the following formula:

$$\text{GPA} = \frac{\sum(\text{grade points obtained in a course} \times \text{total credit for that course})}{\text{total credits taken at a given year}}$$

CGPA = cumulative GPA for different years.

### Promotion to the Next Academic Year

A student has to attend courses required for a particular year, appear at the annual examinations and score a minimum specified GPA/CGPA for promotion to the next year.

Table 2.5: Minimum required GPA/CGPA for promotion to the next academic year year

Promotion	GPA/CGPA	Grade earned
Year 1 to Year 2	2.00	D
Year 2 to Year 3	2.00	D
Year 3 to Year 4	2.00	D

### 2.3.3 Minimum Requirements for the Award of the B.S. Honours Degree in Applied Statistics and Data Science

1. Minimum number of required credits must be earned in the maximum period of six academic years starting from the date of 1<sup>st</sup> year of admission.
2. Must have a CGPA of at least 2.5.
3. A student obtaining an “F” grade in any course (theory or computing) will not be awarded the degree. A student with an “F” grade in any course shall be allowed to retake twice/two times either within three months of publication of the 4<sup>th</sup> year results with special fees or with the following batches.
4. The award of the B.S. (Honours) degree will not depend on the performance on the non-credit course.

#### Some important policies about the examination system

##### 1. In-course Examination

- (a) No make-up test will be arranged for a student who fails to appear in in-course test/tests. Absence in any in-course test will be counted as zero when calculating the average in in-course test for that course. However, a student can apply to the Director if recommended by the respective course teacher. The Director will place the application before the academic committee only if the particular student has met with an accident or her/his parents have expired or s/he has gone through a surgical procedure or any other such situation which the Academic Committee feels can be considered. The make-up test must be held during the course period.
- (b) Course teachers must announce results within four weeks of holding the examinations.
- (c) Marks for in-course assessments must be submitted by concerned course teachers to the Chairman of the Examination Committee and the Controller of Examinations before the final examination.
- (d) Questions for in-course examinations may preferably be of multiple choice (MCQ) types. Students may also be evaluated by giving short questions as decided by the course teacher.

##### 2. Final Examination

- (a) The year final examinations will be conducted centrally by the Controller of Examinations as per existing rules.



- (b) Attendance in the non-credit course will be added in the calculation of average attendance required to appear in final examination.
- (c) Students having 75% or more attendance on average (collegiate) are eligible to appear in the final examination.
- (d) Students having 60%-74% attendance are considered to be non-collegiate and will be eligible to sit for the final examination with a penalty (the amount will be fixed by the Dean, faculty of science).
- (e) Students having attendance less than 60% will not be allowed to sit for the final examination but may seek readmission in the program.
- (f) At the beginning of each academic session, an examination committee is to be constituted for that session by the academic committee of the institute. The Chairman of the Examination Committee will act as a course co-ordinator for that session. The examination committee will have a Chairman, two internal members and an external member.
- (g) For theoretical course final examinations, there will be two examiners: the course teacher will be the first examiner and the second examiner will be a faculty from within the department or from any other department of the University of Dhaka relevant to the subject.
- (h) Third Examination: Under the double-examiner system and in case of difference of more than 20% of marks, there will be a third examination. Marks of the nearest two examiners (theory and project report) will be averaged for the final mark.

### 3. Time Limits for Completion of Bachelor's Degree

A student must complete the courses of her/his studies for a B.S. (Honours) degree in a maximum period of six academic years.

### 4. Improvement

- (a) If a student obtains a grade "C+" or lower in any theoretical course in any year, s/he will be allowed to repeat the term-final examination only once with the following batch for the purpose of grade improvement. However, s/he will not be eligible to get a grade better than "B+" in such a course. A student failing to improve her/his grade in a course can retain the earlier grade.
- (b) Students are not allowed to repeat year final exam for practical courses for the purpose of grade improvement unless he/she obtained "F" grade. Students with only "F" grade in practical courses can give re-take exam to clear "F" for obtaining degree. However, s/he will not be eligible to get a grade better than "B+" in such a course.
- (c) Grade improvement will not be allowed in those courses in which a student obtains a grade better than "C+".
- (d) For the purpose of grade improvement, a student will be permitted to repeat term final examinations for a maximum of 8 (eight) credits in a specific year.
- (e) A student will be allowed to repeat a maximum of 20 (twenty) credits in her/his four years B.S. Program for grade improvement.

- (f) Improvement in the 4<sup>th</sup> year courses: Students would be allowed to sit for improvement examination in the 4<sup>th</sup> year courses with the following batch, provided they must do it before the publication of final result by the office of the Controller of Examinations or Issuance of Provisional Certificate by the Controller of Examinations.
- (g) No improvement for the non-credit course will be allowed.

## 5. Admission to Next Academic Year and Readmission at the Same Year

- (a) A student should take admission to the next academic year within 2 (two) months after publication date of the results of the current year.
- (b) A student (if applicable) can take readmission 2 (two) times throughout the program either in the same class or in different classes. In both cases, s/he must complete the degree by 6 (six) years from the time of original admission.
- (c) A student (if applicable) may seek readmission and continue studies as a regular student provided s/he has at least 30% attendance in the previous year.
- (d) On readmission (if applicable), the student has to retake all courses and examinations. In case s/he does not get the opportunity to repeat the courses due to late admission, marks of in-course assessment and laboratory performance/ assessments in the previous year may be retained by the student. In this case, s/he must retain in-course marks of all previous year courses but not part of the courses.

## 6. Academic Awards

A student can earn the following awards on very successful completion of the degree.

- (a) As a recognition of excellent performance, the names of the students may be included in *Dean's Honor Award* or *Dean's Merit Award* in an academic year without appearing at any improvement examination. There will be two categories of awards for graduate students:
  - i. *Dean's Honor Award*: students with CGPA 3.85 and above (Dean of the faculty of science may change the cutoff).
  - ii. *Dean's Merit Award*: students with CGPA 4.00.
- (b) To be eligible for the ISRT Golden Jubilee award, a student must have a B.S. Honours degree in Applied Statistics and Data Science with the highest CGPA among the students of her/his class without sitting in any improvement examination and have shown outstanding academic merit throughout her/his work for the degree. Note that the student must have completed the degree in four years.

## 7. Other General Regulations

For any matter not covered in the above guidelines, existing rules for Integrated Honours Course of Dhaka University will be applicable.

## 2.4 Academic Year-wise List of Courses

Table 2.6: List of Courses for the First Academic Year

Course ID	Course Title	Credit Hour
AST101	Introduction to Applied Statistics and Data Science	4
AST102	Elements of Probability	4
MATH103	Foundations of Mathematics	3
MATH104	Differential Calculus	3
MATH105	Integral Calculus	3
MATH106	Linear Algebra	3
ECON107	Economics	4
ENG108	English Communication Skills	Non-credit
CSE130	Programming with C/C++	2
CSE131	SQL for Data Science	2
AST140	Oral I	2
Total		30

Table 2.7: List of Courses for the Second Academic Year

Course ID	Course Title	Credit Hour
AST201	Sampling Distributions	3
AST202	Actuarial Statistics	3
AST203	Statistical Inference I	4
AST204	Design and Analysis of Experiments I	3
AST205	Demography	4
AST206	Sampling Methods I	3
MATH207	Mathematical Methods	3
MATH208	Mathematical Analysis	3
AST230	R for Data Science	2
AST231	Statistical Simulation	2
AST232	Statistical Computing I	2
AST240	Oral II	2
Total		34

Table 2.8: List of Courses for the Third Academic Year

Course ID	Course Title	Credit Hour
AST301	Design and Analysis of Experiments II	4
AST302	Sampling Methods II	3
AST303	Linear Regression Analysis	4
AST304	Epidemiology	3
AST305	Lifetime Data Analysis I	3
AST306	Statistical Inference II	3
AST307	Multivariate Statistics I	3
AST308	Research Methodology	3
AST330	Stata for Data Science	2
CSE331	Python for Data Science	2
AST332	Statistical Computing II	2
AST333	Statistical Computing III	2
AST340	Oral III	2
Total		36

Table 2.9: List of Courses for the Fourth Academic Year

Course ID	Course Title	Credit Hour
AST401	Advanced Probability and Stochastic Processes	3
AST402	Statistical Machine Learning	3
AST403	Multivariate Statistics II	3
AST404	Econometric Methods	4
AST405	Lifetime Data Analysis II	3
AST406	Quality Control and Operations Research	4
AST407	Time Series Modelling	3
AST408	Generalized Linear Models	3
AST409	Official Statistics	3
AST430	Statistical Computing IV	2
AST431	Statistical Computing V	2
AST432	Statistical Computing VI	2
AST440	Oral IV	2
AST450	B.S. Capstone Project	3
Total		40

## 2.5 Sustainable Development Goals (SDGs) and B.S. Honours Program in Applied Statistics and Data Science

The Sustainable Development Goals (SDGs) were adopted by all United Nations member states in 2015 as a universal call for action to end poverty, protect the planet, and ensure that all people enjoy peace and prosperity by 2030. There are 17 key SDGs, which have been designed to bring the world to several life-changing ‘zeros’, including zero poverty, hunger, AIDS, and discriminations against women and girls. In Bangladesh, Applied Statistics and Data Science graduates can contribute to achieve SDGs during their future employment potentially through their acquired knowledge of Applied Statistics and Data Science. This is because the scientific knowledge of statistics is welcome by all spheres of development issues particularly in policy making, implementation, monitoring and evaluation. Therefore, it is essential to mark the SDGs indicators in the syllabus for B.S. Honors in Applied Statistics and Data Science so that pertinent course instructor(s) can emphasize on relevant topic(s) for the sake of better understanding of the issues by the learners.

Generally, SDG relevant statistics are recorded, updated, monitored, and evaluated as official statistics by different organs of the government. Principally, government agencies under different ministries are in charge of implementing relevant interventions for achieving different SDGs targets, and Bangladesh Bureau of Statistics (BBS) leads the monitoring of the progress towards meeting the targets through conducting surveys and/or using official statistics. However, as an educational institution Institute of Statistical Research and Training (ISRT) can equip Applied Statistics and Data Science graduates with important statistical and computing skills so that they can work for the government and non-government agencies and help to achieve and monitor the SDGs in future.

Many tools that can be used to compute and evaluate SDG relevant elements are being taught in different courses of B.S. Honors in Applied Statistics and Data Science program, specifically in AST101 (Elements of Applied Statistics and Data Science), ECON106 (Economics), AST202 (Actuarial Statistics), AST205 (Demography), AST206 (Sampling Methods I), AST302 (Sampling Methods II), AST304 (Epidemiology), AST305 (Lifetime Data Analysis I), AST308 (Research Methodology), AST402 (Statistical Machine Learning), AST404 (Econometric Methods), AST405 (Lifetime Data Analysis II), AST406 (Quality Control and Operations Research), AST407 (Analysis of Time Series), AST408 (Generalized Linear Models), and AST409 (Official Statistics). Many of the other theoretical courses such as probability theory (AST102), statistical inference (AST203 and AST302) statistical modeling (AST204, AST301, AST303), multivariate statistics (AST307, AST403), and mathematical courses (MATH103-MATH106, MATH207, MATH208), are also useful for preparing students with a strong foundation of statistical methods related to analyzing real life data (e.g. SDG related data).

Besides theoretical courses, the B.S. Honors in Applied Statistics and Data Science offers a number of statistical computing courses, all of which have been designed to prepare students with the expertise required for statistical analysis of data (e.g. estimation and testing, developing predictive model, etc. required for monitoring and evaluating the progress in achieving SDG targets). In addition, each student of B.S. Honors in Applied Statistics and Data Science is required to write a Capstone Project (AST450), and project works are often related to different SDG indicators. The detailed connectivity among SDG indicators and courses taught in B.S. Honors in Applied Statistics and Data Science have been portrayed in Table

Table 2.10: Connections between SDGs and Courses of B.S. Honours Program in Applied Statistics and Data Science

SDGs	Keywords	Relevant Courses
SDG 1 : End poverty in all its forms everywhere	measuring poverty, zero poverty, poverty line, extreme poverty	101, 106, 206, 308, 450
SDG 2 : End hunger, achieve food security and improved nutrition and promote sustainable agriculture	prevalence of malnutrition among under five children	205, 304, 402, 408, 409
SDG 3 : Ensure healthy lives and promote well-being for all at all ages	reduce neonatal mortality, under five mortality, maternal mortality, death rate	205, 304, 402, 405, 408, 409
SDG 4 : Ensure inclusive and equitable quality education and promote lifelong learning opportunities for all ages	enrollment and dropout rate, participation rate in formal and non-formal education, rate of ICT learning	101, 206, 302, 308, 450
SDG 5 : Achieve gender equality and empower all women and girls	women empowerment, domestic violence, teen marriage	101, 308, 206, 408, 450
SDG 6 : Ensure availability and sustainable management of water and sanitation for all	access to safe drinking water, improved sanitation, hygiene practice	101, 206, 302, 308, 408, 450
SDG 7 : Ensure access to affordable, reliable, sustainable and modern energy for all	access to electricity, population with primary reliance on clean fuels and technology	101, 206, 302, 308, 402, 408, 450
SDG 8 : Promote sustained, inclusive and sustainable economic growth, full and productive employment and decent work for all	GDP, unemployment rate, child labour	101, 106, 206, 308, 402, 407, 450
SDG 10 : Reduce inequality within and among countries	income inequality, poverty line, mapping poverty	106, 206, 308, 450
SDG 13 : Take urgent action to combat climate change and its impacts	climate change, natural disaster	402, 407, 450

1. The course instructors are recommended to point to the key words (Table 1) picked up from SDG in their teaching module(s) wherever appropriate and emphasize relevant tools for teaching the techniques to estimate, test, and evaluate the SDG indicators thereby complying with national goals in line with the targets set in SDGs.

Overall, the B.S. Honors Program in Applied Statistics and Data Science prepares students to tackle any challenges regarding statistical analysis of data, implementation of plans, monitoring and evaluation of intervention programs in real life scenarios. Therefore, Applied Statistics and Data Science graduates will be able to contribute to achieving SDGs, subject to the employment in the pertinent government organs as well as development organizations in Bangladesh.

# 3 Detailed Syllabus

## 3.1 DETAILED SYLLABUS - FIRST YEAR

AST101: INTRODUCTION TO APPLIED STATISTICS AND DATA SCIENCE	Credit 4
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### Introduction

Statistics is about extracting meaning from data. This course will introduce techniques to collect, present, and summarize data to visualize the relationships in data and systematic techniques for understanding the relationships using mathematics. This course will also introduce the data science concept, the ability to extract information from data as a basis for evidence-based decision making is increasingly important in research and work-based situations.

### Objectives

The main objective of this course is to acquaint the students with data science and the typical life cycle of data along with the methods of obtaining and analyzing data in order to make better decisions in an uncertain and dynamic phenomenon. Emphasis will be given mainly on basic statistical methods and techniques for collecting, manipulating, and cleaning data while gaining experience in judging the quality of data sources.

### Learning Outcomes

During this course, students will develop a deeper understanding of the basic underlying features of modern methods of descriptive statistics and equip themselves with a data summarization tool kit which will enable them to apply their knowledge and skills to study other statistics courses and also to apply them in real-world tasks. This course contributes to the following program learning outcomes: (i) demonstrate a solid understanding of data science principles, (ii) demonstrate practical knowledge in data preparation, (iii) knowledge and technical competence, (iv) the ability to use fundamental statistical knowledge, methodologies, and modern computational tools in a suitable and pertinent way, (v) problem-solving, (vi) comprehension of the balance between the difficulty and correctness of the statistical measures used, and the equitability of the delivery of the solution (vii) an ability to amalgam knowledge and compliantly apply them to characterize, analyze and solve a wide range of problems, (viii) personal and professional awareness, (ix) the ability to contextualize outputs where data are drawn from diverse and evolving social, political, and cultural dimensions, (x) the ability to apply lifelong learning principles to new challenges.

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Introduction to data science: data science concept and its life cycle; big data and its sources; explain and demonstrate the value of data in assessing problems and supporting scientific, commercial, social, and artistic problem-solving; distinguish between different types of data that are generated in science, engineering, and design; identify the types of questions that can be asked of data in satisfaction of a particular information goal; Employ strategies for ensuring data quality. Identify aspects of data governance to judge whether and how data can be used in analyses.

Introduction to applied statistics: meaning of statistics; scopes and limitations; concepts of descriptive and inferential statistics; basic concepts: data, sources of data - primary and secondary data; population, sample, parameter, statistic; variables and types of variable: qualitative, quantitative discrete and continuous; scales of measurements; classification of variables by scales of measurements.

Producing data: approaches of producing data; the concept of experimental study and non-experimental study to produce data; introduction to sample survey and questionnaire; the concept of electronically recorded data and hospital recorded data; the concept of data cleaning and checking before statistical analysis.

Organization and presentation of data: graphical presentation for qualitative and quantitative data; sorting data, grouping qualitative and quantitative data: construction of frequency distribution and relative frequency distribution; graphical presentation of frequency distribution histogram, frequency polygon, ogive.

Concept of distribution: location, scale (spread) and shape, illustration with stem-and-leaf diagram; descriptive measures of data; measures of location; measures of dispersion; moments and their interrelationship; measures of skewness and kurtosis; three- and five-number summary; box-plot and modified box-plot.

Description of bivariate data: bivariate frequency distribution; graphical presentation of bivariate data; contingency table; the concept of association between two variables; percentage table and interpretation of cell frequencies; measures of association for nominal and ordinal variables; measures of association for interval or ratio variables; correlation; the relationship between two variables: simple linear regression; basic issues in inferential statistics.

Data visualization and analysis using spreadsheet (e.g., excel, google sheets, etc.).

## Textbooks

1. Weiss N (2007). *Introductory Statistics, 7th edition*. Addison Wesley.

## Reference Books

1. Mann PS (2020). *Introduction to Statistics, 10th edition*. John Wiley & Sons Inc.
2. Newbold P (2004). *Statistics for Business and Economics, 3rd edition*. Prentice-Hall.
3. Witten IH, Frank E, and Hall MA (2016). *Data Science: An Introduction*. John Wiley & Sons Inc.
4. Freeman D, Pisani R, and Purves R (2007). *Statistics, 4th edition*. W.W. Norton and Company.



**Introduction**

This is an introductory course on probability theory. This course attempts to provide basic concepts of set theory, experiment and sample space, and different approaches of defining probability. It discusses useful laws of probability, conditional probability, Bayes rule, random variables and their distributions, and functions of random variables. It also covers discussions on certain operators like mathematical expectation and generating function with properties and applications, and thorough discussions on commonly used probability distributions such as Binomial, Hyper geometric, Negative Binomial, Poisson, Normal, Exponential and Gamma distributions.

**Objectives**

To provide basic concepts of sets, counting techniques, and acquaint students with necessary skills for solving probability related problems using appropriate laws. To introduce the notions of random variables. To develop ability to find probability distribution of random variables and of their functions. To introduce operators like generating functions, expectation, etc. for studying the characteristics of distributions. To make familiar with basic probability distributions with possible areas of applications. To prepare the students for learning advance courses where probability theory has a prominent role.

**Learning Outcomes**

Students who successfully complete this course should be able to: (i) understand the meaning of probability and probability experiment, (ii) use of Venn diagram to represent the result of set operations, (iii) understand the basic probability axioms and rules and the moments of discrete and continuous random variables as well as be familiar with common named discrete and continuous random variables, (iv) know how to derive the probability density function of transformations of random variables and use these techniques to generate data from various distributions, and (v) know how to calculate probabilities, and derive the marginal and conditional distributions of bivariate random variables.

**Contents**

Combinatorial analysis: basic principles of counting, permutations, combinations; axioms of probability: sample space and events, axioms of probability, sample spaces having equally likely outcomes, probability as a measure of belief; conditional probability and independence: conditional probabilities, Bayes formula, independent events.

Random variables: introduction, discrete random variables, expectation, expectation of a function of a random variable, variance, Bernoulli and binomial random variables, Poisson random variable, other discrete random variables (geometric, negative binomial, hypergeometric); expected value of a sum of random variables; properties of cumulative distribution function; continuous random variables: expectation and variance of continuous random variable, normal random variable, normal approximation to binomial distribution, exponential random variables.

Jointly distributed random variables: joint distribution functions, independent random variables, sums of independent random variables, conditional distributions (discrete and continuous cases); properties of expectation: expectation of sums of random variables, covariance, variance of sums, correlations, conditional expectation, moment generating functions, probability generating function.

### Textbooks

1. Ross SM (2009). A First Course in Probability, *8th edition*. Prentice-Hall.

### Reference Books

1. Stirzaker D (2003). Elementary Probability, *2nd edition*. Cambridge.
2. Bertsekas DP and Tsitsiklis JN (2008). Introduction to Probability, *2nd edition*. Athena Scientific.
3. Blitzstein JK and Hwang J (2019). Introduction to Probability, *2nd edition*. Springer.

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MATH103: FOUNDATIONS OF MATHEMATICS
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Credit 3
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### Introduction

The Foundation of mathematics is a course that focuses on three key areas of mathematics: algebra, differential equations, and discrete mathematics. These topics form the building blocks of many areas of mathematics and are essential for understanding advanced topics in statistics, mathematics, and computer science. The course will be taught through a combination of lectures, problem-solving sessions, and hands-on activities.

### Objectives

The objective of the course is to equip students with a solid understanding of the fundamental concepts, theories, and applications of these mathematical areas so that students can develop a strong foundation for advanced topics in statistics and computing.

### Learning Outcomes

After completion of the course, students are expected (i) to learn and understand the theory of numbers and differential equations in detail, (ii) to understand and apply discrete mathematical structures, such as sets, graphs, and combinatorics, to solve problems in computer science, cryptography, and other related fields (iii) to develop problem-solving skills by applying mathematical concepts to real-world problems, (iv) to enhance analytical thinking and logical reasoning skills.

### Contents

#### *Part A (Basic Algebra)*

Theory of numbers: unique factorization theorem; congruences; Euler's phi-function; inequalities: order properties of real numbers; Weierstrass', Chebysev's and Cauchy's inequalities; inequalities involving means; complex numbers: field properties; geometric representation of

complex numbers; operations of complex numbers; summation of algebraic and trigonometric finite series; theory of equations: relations between roots and coefficients; symmetric functions of roots; Descartes rule of signs; rational roots;

Beta and gamma function and their properties; incomplete beta and gamma function ; Dirichlet's theorem.

### *Part B (Differential Equations)*

Formulation of simple applied problems in terms of differential equations; equations of the first order and their solutions; singular solutions; geometric applications; linear equations with constant coefficients; method of undetermined coefficients; variation of parameters, simple cases of linear equations with variable coefficients.

### *Part C (Discrete Mathematics)*

Combinatorics: Counting principles. Inclusion-exclusion principle. Pigeonhole principle. Generating functions. Recurrence relations. Graphs, structure, and symmetry of graphs, trees and connectivity, Eulerian and Hamiltonian graphs and diagraphs, directed graphs, and planar graphs.

Algorithms on graphs: Introduction to graphs, paths and trees. Shortest path problems: Dijkstra's algorithm, Floyd-Warshall algorithm and their comparisons. Spanning tree problems. Kruskal's greedy algorithm, Prim's greedy algorithm and their comparison.

*\*In addition to the compulsory question, students should answer at least one question from each of the part.*

### **Textbooks**

1. Ayres F (1995). Theory and Problems of Modern Algebra. McGraw-Hill.
2. Ross SL (1980). Introduction to Ordinary Differential Equations, *4th edition*. Wiley.
3. Rosen KH (2018). Discrete Mathematics and Its Applications, *8th Edition*. McGraw Hill.

### **Reference Books**

1. Linda Gilbert (2009). Elements of Modern Algebra, *8th Edition*. Brooks/Cole.
2. Stanley J. Farlow (2007). An Introduction to Differential Equations and Their Applications. Dover Publications.

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MATH104: DIFFERENTIAL CALCULUS

Credit 3

### **Introduction**

The course aims to provide a firm foundation in the concepts and techniques of calculus, including basic functions and graphs and their properties, curve sketching, limits, continuity, differentiation, relative extrema, and applications, Taylor Series. This course also introduces calculus from the two-dimensional world of single variable functions into the three-dimensional

world, and beyond, of multivariable functions. Students explore the following topics: vector geometry and the analytic geometry of lines, planes, and surfaces; calculus of curves in two or three dimensions, including arc length and curvature; calculus of scalar-valued functions of several variables, including the gradient, directional derivatives, and the Chain Rule; Lagrange multipliers and optimization problems.

## Objectives

This is a fast-paced course emphasizing computational ability and geometric understanding of calculus. The objective is to provide students with practical mathematical skills necessary for advanced studies in all areas of statistics.

## Learning Outcomes

At the end of the course, the students will be able to (i) interpret a function from an algebraic, numerical, graphical, and verbal perspective and extract information relevant to the phenomenon modeled by the function, (ii) understand the concept of limit and continuity of a function at a point graphically and algebraically using appropriate techniques, (iii) interpret the derivative of a function at a point as the instantaneous rate of change and as the slope of the tangent line, (iv) interpret the value of the first and second derivatives as measures of increase and concavity of a function and understand the consequences of Rolle's theorem and the Mean Value Theorem for differentiable functions, (v) perform operations with vectors in two and three-dimensional space and apply to analytic geometry, (vi) differentiate and integrate vector-valued functions and apply calculus to motion problems in two and three-dimensional space, (vii) determine the limits, derivatives, gradients, and integrals of multivariate functions.

## Contents

Functions and their graphs: polynomial and rational functions, logarithmic and exponential functions, trigonometric functions and their inverses, hyperbolic functions and their inverses, composition of functions.

Limit and Continuity of Functions: Definition. Basic limit theorems, limit at infinity and infinite limits. Continuous functions. Properties of continuous functions on closed and bounded intervals.

Differentiability and related theorems: Tangent lines and rates of change. Definition of derivative. One-sided derivatives. Rules of differentiation. Successive differentiation. Leibnitz theorem. Related rates. Linear approximations and differentials. Rolle's theorem, Lagrange's and Cauchy's mean value theorems. Extrema of functions, problems involving maxima and minima. Concavity and points of inflection. Indeterminate forms. L'Hospital's rule.

Power series expansion: Taylor's theorem with general form of the remainder; Lagrange's and Cauchy's forms of the remainder. Taylor's series. Maclaurin series. 5. Applications: Physical, Biological, Social Sciences, Business and Industry.

Vector-valued functions: Introduction to Vector-Valued Functions, Calculus of Vector-Valued Functions, Tangent lines to graphs of vector-valued functions. Arc length from vector view point. Arc length parameterization.

Curvature: Unit Tangent, Normal and Binormal Vectors, Curvature of plane and space curves: Curvature from intrinsic, Cartesian, Parametric and Polar equations. Radius of curvature.

Centre of curvature.

Partial Differentiation: Functions of several variables, Graphs of functions of two variables, Limits and continuity, Partial derivatives, Differentiability, linearization and differentials. The Chain rule. Partial derivatives with constrained variables, Directional Derivatives and Gradients, Tangent Planes and Normal Vectors, Extrema of functions of several variables, Lagrange multipliers. Taylor's formula for functions of two variables.

### Textbooks

1. Anton H, Bivens I, and Davis S (2012). Calculus, *10th edition*. Laurie Rosatone.

### Reference Books

1. Stewart J (2015). Calculus: Early Transcendentals, *9th edition*. Cengage Learning
2. Swokowski E, Olinick M, and Pence DD (1996). Calculus, *6th edition*. Brooks Cole.

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MATH105: INTEGRAL CALCULUS

Credit 3

### Introduction

This course introduces the student to learn Integral Calculus, the techniques of integration, and to some of the applications of integration to physical problems and finding area, length of curve, volume, and surface area.

### Objectives

The students will be able to (i) interpret the definite integral geometrically as the area under a curve and construct a definite integral as the limit of a Riemann sum, (ii) understand differentiation and anti-differentiation as inverse operations (Fundamental Theorem of Calculus, part 1) and will learn to evaluate integrals using techniques of integration, (iii) understand the different types of improper integrals and solve them, (iv) calculate the area between curves, volumes of solids of revolution, surface area, arc length using integration, (v) solve problems in multiple integrations using rectangular, cylindrical, and spherical coordinate systems, (vi) select and apply appropriate models and techniques to define and evaluate line and surface integrals; these techniques include but are not limited to Green's, Divergence, and Stoke's theorems.

### Learning Outcomes

Upon successful completion of this course, the students will be able to: i) describe the limit and continuity and derivative of a function of single and severable variables, ii) outline the local and absolute extrema of functions and their application, iii) use the concepts of definite and indefinite integrals in a meaningful manner and use appropriate techniques for solving a variety of integration problems involving area, length, surface area, and volume, (iv) determine the area and volume by applying the techniques of double and triple integrals.

## Contents

The anti derivatives (indefinite integral): Techniques of integration; integration by parts; integration by substitution; integration of rational functions, Integration by reduction.

Definite integration: using antiderivatives. Definite integration using Riemann sums. Fundamental theorems of calculus. Basic properties of integration.

Applications of integration: Plane areas. Solids of revolution. Volumes by cylindrical shells. Volumes by cross-sections. Arc length and surface of revolution.

Improper integrals: Improper integrals of different kinds. Gamma and Beta functions.

Integrals in polar coordinates: Area and arc length in polar coordinates.

Double Integrals: Double Integrals over Nonrectangular Regions, Double Integrals in Polar Coordinates, Surface Area; Parametric Surfaces and Applications of Double Integrals.

Triple integrals: Volume as a triple integral, Triple Integrals in Cylindrical and Spherical Coordinates, Centers of Gravity Using Multiple Integrals and Applications of Triple Integrals, Change of Variables in Multiple Integrals; Jacobians.

Topics in vector calculus: Vector Fields, Gradient, Divergence, curl and their physical meanings Line Integrals, Green's Theorem, Surface Integrals, The Divergence Theorem, Stokes' Theorem, Applications of Surface Integrals; Flux.

## Textbooks

1. Anton H, Bivens I, and Davis S (2012). Calculus, 10th edition. Laurie Rosatone.

## Reference Books

1. Stewart J (2015). Calculus: Early Transcendentals, *9th edition*. Cengage Learning
2. Swokowski E, Olinick M, and Pence DD (1996). Calculus, *6th edition*. Brooks Cole.

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MATH106: LINEAR ALGEBRA
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Credit 3
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## Introduction

Linear algebra can be used in pretty much any application that deals with more than random variable at a time than dealing with a random vector. Particularly, linear algebra will be heavily used in multivariate statistics course(s). Some matrix algebra will also be very convenient for potential studies in Markov chains and stochastic processes. Linear regression is a very common use of linear algebra as well.

## Objectives

Solve systems of linear equations using various methods including Gaussian and Gauss-Jordan elimination and inverse matrices. Perform matrix algebra, determinants and their properties. Understand real vector spaces and subspaces and apply their properties. Understand linear independence and dependence. Find basis and dimension of a vector space. Find eigenvalues and eigenvectors and use them in applications. Diagonalize, and orthogonally diagonalize

symmetric matrices. Evaluate the dot product, norm, angle between vectors, and orthogonality of two vectors in  $R_n$ . Compute inner products on a real vector space and compute angle and orthogonality in inner product spaces. Create orthogonal and orthonormal bases: Gram-Schmidt process and use bases and orthonormal bases to solve application problems.

### **Learning Outcomes**

After successfully completion of this course the students will be able (i) to solve systems of linear equations using various methods including Gaussian and Gauss-Jordan elimination and inverse matrices, (ii) perform matrix algebra determinants and their properties, (iii) understand real vector spaces and subspaces and apply their properties. Understand linear independence and dependence, (iv) find basis and dimension of a vector space, (v) find eigenvalues and eigenvectors and use them in the applications, (vi) diagonalize, and orthogonally diagonalize symmetric matrices, Evaluate the dot product, norm, angle between vectors, and orthogonality of two vectors, (vii) compute inner products on a real vector space and compute angle and orthogonality in inner product spaces, (viii) create orthogonal and orthonormal bases: Gram-Schmidt process and use bases and orthonormal bases to solve application problems.

### **Contents**

Matrices, vectors and their operations: basic definitions and different types of matrices, matrix operations (addition, multiplication), trace of a matrix, determinant and adjoint of a square matrix, properties of determinants, inverse of matrix, properties of inverse, Kronecker product and related operations.

System of linear equations: Gaussian elimination, Gauss-Jordan elimination, homogeneous linear systems, null spaces and the general solution of linear systems, rank and linear systems, generalized inverse of a matrix, generalized inverses and linear systems.

Vector spaces and subspaces: vector addition and scalar multiplication, linear spaces and subspaces, intersection and sum of subspaces, linear independence and dependence, basis and dimension, inner product, norms and orthogonality, orthogonal projections, Gram-Schmidt orthogonalization.

Eigenvalues and eigenvectors: eigenvalue equation, characteristic polynomial and its roots, Eigenspaces and multiplicities, diagonalizable matrices, computation of eigenvalues and eigenvectors.

Singular value and Jordan decompositions: singular value decomposition, SVD and linear systems, computing the SVD, Jordan canonical form.

Quadratic forms: matrices in quadratic forms, positive and nonnegative definite matrices, congruence and Sylvester's law of inertia, nonnegative definite matrices and minors, some inequalities related to quadratic forms, simultaneous diagonalization and the generalized eigenvalue problem.

### **Textbooks**

1. Anton H and Rorres C (2013). *Elementary Linear Algebra, 11th edition*. Wiley.

### **Reference Books**

1. Strang G (2023). *Introduction to Linear Algebra, 4th edition*. Wellesley-Cambridge.

2. Banerjee S and Roy A (2014). Linear Algebra and Matrix Analysis for Statistics. Chapman and Hall/CRC
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ECON107: ECONOMICS

Credit 4

## Introduction

This course provides an introduction to a broad range of economic concepts, description of theories and analytical techniques. It considers both microeconomics: the supply and demand based choices made by individual units (households and firms), and macroeconomics: the broader analysis of the economy. The use of supply and demand models will be the fundamental tools and the trade-offs and choices will be considered through comparison of costs and benefits measures. Production and market structure will be analyzed at the firm level as well. Macroeconomic issues concerning the interaction of goods and services markets, labor supply and economic resources at an aggregate level (region or country level) will be discussed.

## Objectives

On successful completion of this course, students will be able to: explain how microeconomic models can be used to consider fundamental economic choices of households and firms; describe how macroeconomic models can be used to analyze the economy as a whole; interpret economic models, diagrams and tables and use them to analyze economic environment; illustrate how government policy influences microeconomic choices and macroeconomic upshots.

## Learning Outcomes

After completion of the course, students are expected to (i) understand theories and principles in microeconomics including price theory, market structure, trade-offs, comparative advantage, factor markets, consumer theory, public goods, externalities and market failure, (ii) apply these principles to analyze economic issues, acquire quantitative skills used in economic analyses, (iii) understand fiscal policy and monetary policy of Bangladesh and address SDG goals.

## Contents

Definition and scope of economics; theory of demand and supply; demand schedule; supply schedule; equilibrium of demand and supply; elasticity of demand and supply: measurement of elasticity; price elasticity of demand and supply.

Demand and consumer behavior; utility theory; equi-marginal principle; indifference curve analysis: consumers surplus; individual and market demand; derivation of demand curve; theory of production: production function; total, average and marginal product; law of diminishing returns; factors of production; pricing of factors of production; division of labor; localization of industries; returns to scale; law of variable proportion; isoquants; Cob-Douglas and CES production function; theory of cost; fixed and variable cost; total and marginal costs; least cost rule; opportunity cost.

Market structure: perfect and imperfect competition; pricing under monopoly, oligopoly and monopolistic competition; short-run and long-run equilibrium analysis; income and wealth:



factor incomes vs. personal incomes, role of government, wealth; fundamentals of wage determination, the supply of labor, determinants of supply, empirical findings, wage differentials; basic concepts of interest and capital, prices and rentals on investments, rates of return and interest rates, present value of assets, real vs. nominal interest rates.

Key concepts of macroeconomics: objectives and instruments of macroeconomics; measuring economic success, tools of macroeconomic policy; real vs. nominal GDP, “Deflating” GDP by a price index; consumption, investment, NDP, GNP, price indexes and inflation; consumption and saving: consumption function, saving function; investment: determinants of investment, revenues; theories of economic growth: four wheels of growth, human and natural resources, capital; theories of economic growth: classical dynamics of Smith and Malthus, neoclassical growth model.

Index number: characteristics and uses, problems in the construction, classification; methods: unweighted, weighted: Laspeyre’s, Paasche’s, Dorbish and Bowley’s, Fisher’s, Marshall and Edgeworth’s, Kelly’s and the chain index numbers; test of accuracy, base shifting, splicing, deflating of index numbers; application of consumer price index number.

### **Textbooks**

1. Samuelson PA and Nordhaus WD (2009). *Economics, 19th edition*. McGraw Hill.

### **Reference Books**

1. Mankiw NG (2015). *Principles of Economics, 7th edition*. Cengage Learning.
2. Dowling ET (2011). *Introduction to Mathematical Economics, 3rd edition*. McGraw-Hill Education.
3. Newbold P, Carlson W and Thorne B (2012). *Statistics for Business and Economics, 8th edition*. Pearson.

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ENG108: ENGLISH COMMUNICATION SKILLS

Non-credit

### **Introduction**

English is the language of our international communication in all areas. Having a good command of English helps the graduate to have more opportunities in life, first of all, their career. Strong communication in English involves four modes: reading, writing, speaking, and listening. Different people have naturally differing aptitudes for these skills.

### **Objectives**

The aim of this course is to develop the student’s ability to use English effectively for the purpose of practical communication. The course aims to expand vocabulary, increase proficiency in reading, writing and listening and develop greater understanding of grammatical rules and usage. It therefore has four components: Writing, Reading, Listening and Speaking.

### **Learning Outcomes**

After completion of this course students are expected to learn the followings:

Reading: Develop critical reading skills; identify and retrieve facts and details; understand and select relevant information; recognize and understand ideas, opinion, attitudes and connections between related ideas; understand what is implied but not actually written; infer and predict meanings.

Writing: Communicate clearly, accurately, appropriately and express opinions effectively; summarize, paraphrase, synthesize and apply logical reasoning; employ and control a variety of grammatical structures; demonstrate knowledge and understanding of a range of appropriate vocabulary; apply the conventions of sentence construction, paragraphing, punctuation, spelling and academic referencing.

Listening: Identify and retrieve facts and details; recognize and understand ideas; opinions, attitudes and connections between related ideas, develop and apply basic skills of a good listener. Speaking: Communicate clearly, accurately and appropriately; convey information and express opinions effectively; employ and control a variety of grammar structures; demonstrate knowledge of a range of appropriate vocabulary, engage in conversation, employ suitable pronunciation.

## **Contents**

Reading: Reading comprehension and application of reading strategies; Skimming and scanning texts to identify and retrieve facts, details, important points and themes; Recognizing ideas, opinions and attitudes in a range of texts such as letters, brochures, forms, imaginative writing, reports, academic papers and creative essays; Developing critical reading skills (e.g., paying attention to different perspectives exposed in texts); Extending reading opportunities to build vocabulary; Learning differences between formal and informal writing.

Writing: Structure of a paragraph, writing process of narrative and descriptive paragraphs; Learning how to summarize, paraphrase, synthesize and apply logical reasoning; Sentence variety: simple, compound and complex sentences; Getting familiar with/revising basic grammar through literary texts, newspaper articles, short excerpts.; Common sentence errors: Subject/verb agreement, incorrect verb forms, shift in tense, shift in point of view, unclear or missing referent, lack of pronoun agreement, etc.; Punctuation errors; Academic referencing; Carrying out simple writing tasks (e.g., writing essays on a given topic, writing emails/letters, etc.) in an appropriate and accurate form of English.

Listening: Understanding simple information presented in a variety of forms, e.g. news, weather, dialogue, interviews and telephone conversations; Learning to develop and apply basic skills of a good listener (e.g. grasping the main idea of a text, taking notes); Identifying and retrieving some facts from materials e.g. a formal talk, monologues, lectures, etc.; Understanding what is implied but not actually spoken e.g., gist, purpose and intention;

Speaking: Basics of everyday communication; Carrying out a range of speaking activities such as introducing oneself, participating in short debates, engaging in conversation in different environments e.g., while shopping, meeting friends, travelling, visiting a doctor, answering the telephone, etc.; Conducting a sustained conversation with a sense of audience and purpose; Effective use of communication strategies to share knowledge or participate in group/pair discussions; Learning and practicing basic pronunciation skills (IPA symbols, diphthongs, monophthongs, long and short vowels); Developing presentation skills.

## Textbooks

1. Bailey S (2003). Academic Writing: A Handbook for International Students. Routledge.
2. Soars L and Soars J (2003). Headway Intermediate. Oxford University Press.

## Reference Books

1. Langan J (1984). College Writing Skills with Readings. Connect.
2. Roach P (2009). English Phonetics and Phonology: A Practical Course, *4th edition*. Cambridge University Press.
3. O'Connor JD (1980). Better English Pronunciation. Cambridge University Press.
4. Cambridge IELTS

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CSE130: PROGRAMMING WITH C/C++
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Credit 2
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## Introduction

Programming with C/C++ course mainly focuses the programming language C. The course introduces machine level language, origin of C and applications of C programming in statistics.

## Objectives

This module covers introductory ideas how to connect C programming with statistics through flowchart and programing code execution using compilation, link and run. To understand how to analyses descriptive statistics and data analysis using C programming.

## Learning Outcomes

This course is expected to enable students to achieve understanding (i) how to connect C programming with statistics through flowchart and programing code execution using compilation, link and run (ii) how to analyse descriptive statistics and data analysis using C programming.

## Contents

Introduction to programming: algorithm, flowchart, code (program); levels of programming: machine level, assembly level and high level language; execution of code: translator, compiler, interpreter, assembler; steps of execution: compilation, link, run.

An overview of C: the origins of the C language, compilers versus interpreters; variables, constants, operators, and expressions: data types, declaration of variables, assignment statements, constants, operators, expressions; program control statements: C statements, conditional statements, loop statements, labels; functions: the return statement, function arguments, arguments to main(), returning pointers, pointers to functions; arrays: single-dimension arrays, passing single dimension arrays to functions, two- and multi-dimensional arrays, arrays and pointers, allocated arrays, array initialization.

Applications of C programming in data analysis: frequency distributions, data summary, e.g. mean, median, maximum, minimum, matrix operations, calculation of different rates, fitting simple linear regression and sorting a vector.

## Textbooks

1. Dietel PJ and Deitel HM (2010). C How to Program, *7th edition*. Pearson.

## Reference Books

1. Perry G and Miller D (2014). C Programming Absolute Beginner's Guide, *3rd Edition*. Que.

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CSE131: SQL FOR DATA SCIENCE
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Credit 2
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## Introduction

In today's data-driven world, business enterprises and industries can access more data than ever. However, they need skilled professionals who can manage and analyze data using various tools and techniques to make sense of all this data. Structured Query Language (SQL) is a widely used tool in data science for managing and querying data stored in relational databases. This course is designed to introduce students to SQL and its application in data science.

## Objectives

The objectives of this course are to teach students the basics of SQL through hands-on exercises and real-world examples, including how to create tables, insert and update data, and retrieve information using SQL statements in databases. This course will also cover more advanced topics such as SQL joins, subqueries, and aggregation functions. By the end of this course, students will have acquired a comprehensive understanding of SQL and its pivotal role in data science.

## Learning Outcomes

Upon the completion of this course, students are expected to (i) understand the basic concepts of SQL, such as tables, queries, and basic SQL syntax; (ii) retrieve and manipulate data from databases using SQL queries, including filtering, sorting, and joining data from multiple tables; (iii) perform basic data analysis using SQL, including calculating summary statistics and aggregating data, (iv) Understand how SQL fits into the data science workflow.

## Contents

Introduction to databases, SQL and MySQL, creating a MySQL database, MySQL Data types, table creation, Populating and modifying tables, When Good Statements Go Bad, query mechanics.

The select, from, where, group by, order by, and having clauses.

SQL joins, subqueries, common table expressions, aggregation functions, window functions, date and time functions, and user-defined functions (UDFs).

Calculating summary statistics, univariate and bivariate frequency distributions, correlation, and regression analysis.

### **Textbooks**

1. Beaulieu A. (2020). Learning SQL: Generate, manipulate, and retrieve data, *3rd edition*. O'Reilly.

### **Reference Books**

1. Teate RM (2021). SQL for data scientists: A beginner's guide for building datasets for analysis. Wiley.

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AST140: ORAL I

Credit 2

Each student must be examined by a committee of selected members at the end of the academic year.

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## 3.2 DETAILED SYLLABUS - SECOND YEAR

AST201: SAMPLING DISTRIBUTIONS

Credit 3

### Introduction

This course introduces the theory of probability and sampling distribution for describing the behavior of random processes and further concentrates on using sampling distributions in statistical inference. Contents will involve deriving the theoretical properties of different distributions, examining the inter-relationship between them, and focusing on their applications for exploratory analysis regarding selecting appropriate distributions for explaining the random behavior based on data and statistical inference.

### Objectives

This course's main objective is to acquaint students with the main concepts and uses of probability and sampling distributions in the theory of statistical inference. More specific objectives include demonstrating the derivation and approximation of sampling distributions of sample statistics, describing properties of common sampling distributions, and illustrating the role and use of sampling distributions in inferential statistics.

### Learning Outcomes

Upon completion of the course, students should (i) get acquainted with the main theoretical concepts probability and sampling distributions, (ii) learn about different generating function techniques and their role in mathematical derivation of distributions of functions of random variables, (iii) understand the role of the law of large numbers in approximating sampling distributions, (iv) learn about mathematical properties of common sampling distributions and inter-relationships and (v) understand the application of sampling distribution in statistical inference.

### Contents

Generating function techniques: moment generating function, cumulant generating function, probability generating function, characteristic function; finding distributions of functions of random variables: change of variable technique, distribution function technique, and moment-generating function technique; probability integral transformation; statistic and sampling distribution; law of large numbers; central limit theorem; exact distribution of sample mean; chi-square distribution and its properties; F-distribution and its properties; t-distribution and its properties; non-central chi-square, F and t distributions: definition and derivation; concept of order statistics, distributions of single order statistics, and joint distribution of two or more order statistics.

A brief review of some probability distributions and their properties: uniform, normal, exponential, gamma, beta, log-normal, Cauchy; definition of truncated distribution; definition of compound and mixture distribution; family of distributions: Pearsonian distribution.

### Textbooks

1. Robinson EA (2011). Probability Theory and Applications. Springer.

## Reference Books

1. Zehna PW (1970). Probability Distributions and Statistics. Allyn and Bacon.
2. Jones O, Maillardet R and Robinson A (2009). Introduction to Scientific Programming and Simulation using R. Chapman & Hall/CRC.
3. Arnold BC, Balakrishnan N and Nagaraja HN (2008). A First Course in Order Statistics. Society for Industrial and Applied Mathematics.

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AST202: ACTUARIAL STATISTICS
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Credit 3
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## Introduction

This course aims at providing an introduction to principles of actuarial science and mathematics involved in it. Topics include role of insurance in economy, different instruments involved in actuarial computations including interest and discount rates, pricing and valuation of actuarial products including annuities, amortization schedules, sinking funds, life assurances and premiums, among others.

## Objectives

The course will enable understanding of the fundamental concepts of actuarial science and appreciate its role in economy. It will build a concrete knowledge of underlying theories behind actuarial computations. Finally, it will help to understand how statistical and mathematical models are used in pricing and valuing actuarial products and their real life applications.

## Learning Outcomes

Upon completion of this course the students should be able to (i) understand the fundamental concepts of actuarial science and appreciate its role in economy, (ii) obtain concrete knowledge of underlying theories behind actuarial computations and (iii) understand how statistical and mathematical models are used in pricing and valuing actuarial products and their applications in various real-life actuarial problems.

## Contents

The meaning of actuarial science; role of insurance in the economy; role of an actuary.

Fundamentals of theory of interest: definition of simple interest and compound interest and their comparisons; accumulated value factors and present value factors; effective and nominal rates of interest and their interrelationship; effective and nominal rates of discount; relation between interest and discount; equations of value and use of the time diagram in solutions of problems in interest; problems involving unknown length of investment and unknown rate of interest; annuity; different types of annuities certain; present and accumulated values of immediate annuity and annuity due; present value of deferred annuities and variable annuities; capital redemption policies; amortization schedules and sinking funds.

Actuarial mathematics: discrete life annuity and its applications; present values of different life annuities; life assurance; present values of various life assurances in terms of commutation functions; related problems; premiums; different types of premiums; net premiums; office premiums; prospective policy values.

The basic deterministic model: cash flows; an analogy with currencies; discount functions; calculating the discount function; interest and discount rates; constant interest; values and actuarial equivalence; regular pattern cash flows; balances and reserves; basic concepts; relationship between balances and reserves.

Stochastic interest-rate models: stochastic interest-rate models I; basic model for one stochastic interest rate; independent interest rates; stochastic interest-rate models II; dependent annual interest rates; modelling the force of interest; what one can do with these models.

### Textbooks

1. Kellison SG (1991). *The Theory of Interest, 2nd edition*. McGraw-Hill/Irwin.
2. Promislow SD (2011). *Fundamentals of Actuarial Mathematics, 2nd edition*. John Wiley & Sons.

### Reference Books

1. Shailaja R. Deshmukh (2010). *Actuarial Statistics: An Introduction Using R, 3rd edition*. Orient Blackswan.

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AST203: STATISTICAL INFERENCE I
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Credit 4
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### Introduction

This course deals with fundamental concepts and techniques of statistical inference including estimation and tests of simple and composite hypotheses. A brief revision will also be given of some basic topics in probability theory as well as random variables.

### Objectives

The aim of the course is to provide a thorough theoretical grounding in statistical inference. The primary objective is to provide an introduction to mathematical statistics necessary for the subsequent study of specialized courses in statistics, bio-statistics, actuarial science and econometrics. The impact that statistics has made and will continue to make in virtually all fields of scientific and other human endeavours is considered.

### Learning Outcomes

After completing the course, the students are expected to (i) know the most common parametric and non-parametric distributions, (ii) be familiar with the concept of the likelihood principle, get used to the maximum likelihood, least square and the method of moments, (iii) be able to handle a parametric hypothesis testing problem, and (iv) to use the likelihood ratio method, have some knowledge of asymptotic statistics, that would help them to estimate and predict the SDG indicators upon the availability of baseline and midterm data with intervention.

### Contents

Basic Concepts: Fundamental ideas of statistical inference; parametric and non-parametric inference; estimators, statistics, parameters, theory and reality; sampling distributions and uses



in inference; Estimation: Estimation of parameters and fitting of probability distributions; parameter estimation: method of moments, method of least squares, method of maximum likelihood - properties of maximum likelihood estimators, Bayes estimator; properties of a good point estimator; method of evaluating estimators: mean squared error; best unbiased estimator - efficiency and the Cramer-Rao lower bound; sufficiency - sufficient statistics, properties of sufficient statistics, exponential family and factorization theorem, the Rao-Blackwell theorem, minimal sufficient statistics, complete statistics.

Interval estimation: introduction; method of constructing confidence interval - pivotal quantity, exact and approximate confidence interval; large- and small-sample confidence intervals; selecting the sample size; simultaneous confidence region.

Test of Hypothesis: Elements of statistical hypothesis test; approaches to hypothesis testing: Neyman-Pearson approach, Fisher approach, and Jeffreys' approach; common tests based on normal distribution: one-sample settings, two-sample (independent and paired) settings, more than two sample settings; the duality of confidence intervals and hypothesis tests; exact and large sample test; evaluating statistical test procedure - the power of tests, optimal test - Neyman-Pearson lemma; most powerful tests; composite hypotheses; generalized likelihood ratio test; uniformly most powerful tests; unbiased tests; goodness-of-fit tests - probability plots, test for normality, chi-square goodness of fit test, Kolmogorov-Smirnov test; statistical tests applied to categorical data problems: introduction, Fisher's exact test, the chi-square test of homogeneity, chi-square test of independence.

### **Textbooks**

1. Hogg RV, Tanis EA and Zimmerman DL (2015). Probability and Statistical Inference, *9th edition*. Pearson.

### **Reference Books**

1. Casella G and Berger RL (2001). Statistical Inference, *2nd edition*. Cengage Learning.
2. Hogg RV, McKean J and Craig AT (2010). Introduction to Mathematical Statistics, *7th edition*. Pearson.
3. Mood AF, Graybill FA. and Boes DC (1973). Introduction to the Theory of Statistics, *3rd edition*. McGraw-Hill.

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AST204: DESIGN AND ANALYSIS OF EXPERIMENTS I
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Credit 3
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### **Introduction**

This course covers methodological and practical issues to design and analysis of experiments. Topics covered will include an introduction to design of experiments, completely randomised design, randomised complete block design, Latin square design and balanced incomplete block design.

### **Objectives**

The course will help to understand the methodological issues of experimental design. Students will develop an understanding to write hypotheses that can be tested using experiments.

Finally, it will build a base to analyse and interpret data obtain from experiments.

## Learning Outcomes

After completing the course, the students are expected to (i) identify the response variable, factor(s) of interest and nuisance factors, (ii) choose the most suitable experimental design for the given problem, (iii) set up the relevant null and alternative hypotheses. Obtain ANOVA tables, draw appropriate conclusions from them, (iv) construct appropriate (orthogonal) contrasts, test their significance and make conclusions, (v) carry out multiple comparisons among them and make recommendations, (vi) check model assumptions graphically and formally and apply a suitable transformation when needed, (vii) find the appropriate sample size, and (viii) analyze data and state conclusions in the language of the problem posed.

## Contents

Introduction to design of experiments: strategy of experimentation; some typical examples of experimental design; basic principles; guidelines for designing experiments.

Experiments with a single factor: the analysis of variance; analysis of fixed effects model; estimation of model parameters; unbalanced data; model adequacy checking; regression model, comparisons among treatment means, graphical comparisons of means, contrasts, orthogonal contrasts, multiple testing, Scheffe's method, comparing pairs of treatment means, comparing treatment means with a control; Determining sample size; operating characteristic curve, specifying standard deviation increase, confidence interval estimation method; discovering dispersion effects; regression approach to analysis of variance; least squares estimation of the model parameters, general regression significance test.

Randomized blocks, Latin squares, and related designs: the randomized complete block designs (RCBD); statistical analysis of RCBD, model adequacy checking; estimating model parameters; Latin square design; Graeco-Latin square design; balanced incomplete block design (BIBD); statistical analysis of BIBD; least squares estimation of BIBD; recovery of intra-block information in the BIBD.

## Textbook

1. Montgomery DC (2019). Design and Analysis of Experiments, *10th edition*. Wiley.

## Reference Books

1. Dean AM, Voss AM, and Draguljić (2017). Design and Analysis of Experiments, *2nd edition*. Springer.
2. Bailey R (2008). Design of Comparative Experiments. Cambridge.

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AST205: DEMOGRAPHY
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Credit 4
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## Introduction

Demographic data contains valuable information about a country's socio-economic development, population growth and trend as well as the overall public health scenario. Thus Demographic data comprises significant importance both in statistics and public health arena.

This course focuses on defining the demographic life events and explains the statistical analysis procedures.

### **Objectives**

The course is intended to introduce the basic ideas of demography and state the importance of demographic studies. It helps to understand well-known demographic theories and different measures of demographic events. Students will perceive and analyze current demographic situation of Bangladesh.

### **Learning Outcomes**

Upon successful completion of the course the students are expected to know (i) demographic data sources and collection procedure (ii) compute and interpret different types of fertility data (iii) measure different mortality statistics (iv) nuptiality measures (v) migration statistics and effect on population growth

### **Contents**

The basic concept of demography; role and importance of demographic/population studies; sources of demographic data: census, vital registration system, sample surveys, population registers, and other sources, especially in Bangladesh.

Errors in demographic data: types of errors and methods of testing the accuracy of demographic data; quality checking and adjustment of population data; post-enumeration check (PEC) and detection of errors and deficiencies in data and the needed adjustments and corrections.

Fertility: basic measures of fertility, crude birth rate, age-specific fertility rates (ASFR), the general fertility rate (GFR), the total fertility rate (TFR), the gross reproduction rate (GRR), and net reproduction rate (NRR), child-woman ratio; the concept of fecundity and its relationship with fertility. Fertility trends and patterns in Bangladesh.

Demographic theory: transition theory and the present situation in Bangladesh; Malthus' theory and its criticism. Mortality: basic measures of mortality: crude death rate (CDR), age-specific death rates (ASDR), infant mortality rate, child mortality rate, neonatal mortality rate; standardized death rate its need and use; direct and indirect standardization of rates; commonly used ratios: sex ratio, child-woman ratio, dependency ratio, and density of population. Mortality trends and patterns in Bangladesh.

Nuptiality: marriage, types of marriage, age of marriage, age at marriage and its effect on fertility, celibacy, widowhood, divorce, and separation, their effect on fertility and population growth.

Migration: definition, internal and international migration; sources of migration data; factors affecting both internal and international migration, laws of migration; the impact of migration on origin and destination, its effect on population growth, age and sex structure, labor supply, employment and unemployment, wage levels, and other socio-economic effects; migration of Bangladeshis abroad and its impact on the overall economic development of the country.

Graduation of data: meaning and its need, techniques of graduation, graduation of age distribution; life table: its concept, structure, and calculation; complete life table (life table by single year of age) and abridged life table, multiple decrement life tables, working life table,

different life table functions and inter-relationships among them, use of life table, etc. Model life tables, Coale and Demeny regional model life tables.

Stable and stationary populations.

### Textbooks

1. Siegel JS and Swanson DA (2004). *The Methods and Materials of Demography, 2nd edition*. Emerald.
2. Shryock HS, Siegel JS and Larmon EA (1975). *The Methods and Materials of Demography, volume I and II*. U.S. Department of Commerce Publication.

### Reference Books

1. Poston Jri. DL, and Bouvier LF (2016). *Population and Society: An Introduction to Demography, 2nd edition*. Cambridge University Press.

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AST206: SAMPLING METHODS I
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Credit 3
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### Introduction

This course introduces basic sampling techniques used in sample survey along with estimation procedures. This course covers simple random sampling, systematic sampling, stratified random sampling, and cluster sampling. It also covers some special sampling designs.

### Objectives

To make students familiar with different sampling techniques so that they can determine required sample size and choose appropriate sampling techniques for a real life survey situation.

### Learning Outcomes

After completion of the course students are expected to (i) know about the necessity of sample survey, (ii) steps of conducting a survey, (iii) different approaches to design a survey (iv) determine sample size, (v) and estimation techniques for the population parameters of interests.

### Contents

Introduction: concept of sampling, and definition of related terms; role of sampling theory, requirements of a good sampling design, steps in a sample survey, probability and nonprobability sampling, selection (draw-to-draw) and inclusion probability, sampling weight, with and without replacement sampling, characteristics of estimate: bias, mean square error and variance (precision), errors in sample survey and census, sample size determination: basics and complex scenarios.

Simple random sampling (SRS): sample selection, estimation: mean, total, proportion, ratio of two quantities, unbiasedness and variances/standard errors (SEs) of the estimators, estimators of the SEs, confidence interval (normal approximation); finite population correction, estimation over subpopulation, computation: inclusion probabilities and sampling weights.

Systematic sampling: motivation, use and challenges, sample selection, different estimators and their unbiasedness and variances, estimator of the variances, comparison with SRS, sampling from population with linear trend or periodic variation.

Stratified random sampling: concept, reasoning and needs in heterogeneous population, number and formation of strata, sample selection, estimators (total, mean, proportion), variances of the estimators, estimators for the variances, different allocation techniques, comparison with SRS, design effect and its uses, poststratification, quota sampling.

Auxiliary information in estimation: ratio estimators (total, mean), different properties: unbiasedness, variance (approximate), estimated variance, confidence interval, comparison with mean per unit estimates, conditions for best linear unbiased ratio estimator, application in stratified sampling, unbiased ratio-type estimates; product estimator; regression estimator: linear regression estimate and its properties (unbiasedness, variance and estimated variance) under preassigned  $b$  and estimated  $b$ , comparison with mean per unit estimate, application in stratified sampling, relative merits and demerits.

Cluster sampling: motivation and reasoning, formation and size of clusters; cluster sampling with equal sized clusters: estimators and their various properties (unbiasedness, variance and estimated variance), comparison with SRS and systematic sampling, optimum cluster size, stratification in cluster sampling: estimation and comparison with simpler sampling designs.

Special sampling designs: capture-recapture sampling: implementation, Peterson and Chapman estimators for population size and their variances, Hypergeometric and Multinomial models for estimating population abundance; ranked set sampling: sample selection and estimation.

### Textbooks

1. Thompson SK (2002). *Smampling. 2nd edition.* Wiley.
2. Cochran WG (1977). *Sampling Techniques, 3rd edition.* Wiley.

### Reference Books

1. Lohr SL (1998). *Sampling: Design and Analysis.* Duxbury.
2. Levy PS and Lemeshow S (2008). *Sampling of Populations: Methods and Applications, 4th edition.* Wiley.
3. Rao PSRS (2000). *Sampling Methodologies with Applications, 1st edition.* Chapman & Hall/CRC.
4. Thompson SK (2012). *Sampling, 3rd edition.* Wiley.

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MATH207: MATHEMATICAL METHODS

Credit 3

### Introduction

This course presents mathematical and elements of scientific computing approach for solving mathematical problems that arises mainly in science and engineering applications. It deals

with the theory and application of numerical approximation technique as well as their computer implementation. Mathematical methods, mainly Fourier analysis and Laplace transform, provide a foundation for further studies in disciplines in which Mathematics and Statistics may play important roles.

### **Objectives**

The course wants to develop an understanding of the core idea and concepts of numerical methods. It will enable applying rigorous analytic, highly numerate approach and developing scientific computer programs. Students will also develop the ability to apply Fourier series and Fourier Integrals to significant applied problems especially in telecommunication that are closely related to Laplace transform.

### **Learning Outcomes**

Upon completion of this course the students should be able to (i) apply rigorous analytic, highly numerate approach and develop scientific computer programs, (ii) develop the ability to apply Fourier series and Fourier Integrals to applied problems, and (iii) understand and apply in telecommunication that is closely related to Laplace transform.

### **Contents**

Interpolation and inverse interpolation: uses of Newton's forward and backward interpolation formula; Lagrange's formula; numerical integration: Simpson's rule; Weddle's rule; trapezoidal rule; Gauss's quadratic formulae and proper examples from the applications to econometrics, meteorology and biomedicine; Euler's formula of summation and quadrature.

Solution of numerical algebraic and transcendental equations; equations in one unknown; finding approximate values of the roots; finding roots by repeated application of location theorem; method of interpolation or of false position; solution by repeated plotting on a large scale; Newton-Raphson method; Newton-Raphson method for simultaneous equations.

Fourier series: periodic function; Fourier series process of determining the Fourier coefficients; Dirichlet conditions; odd and even functions; half range Fourier sine or cosine series; Parseval's identity; differentiation and integration of Fourier series.

Laplace transform: introduction; definition of integral transformation; definition of Laplace transform; Laplace transform of some elementary functions; sufficient conditions for the existence of Laplace transform; some important properties of Laplace transform; initial and final value theorem; Laplace transforms of some special functions.

Inverse Laplace transform: definition of inverse Laplace transform; Lerch's theorem; some important properties of the inverse Laplace transform; partial function decompositions; definition of convolution; convolution theorem; Heaviside's expansion formula; evaluation of integrals; application of Laplace transform.

Introduction to Taylor's and Laurent series.

### **Textbooks**

1. Burden RJ and Faires JD (2010). Numerical Analysis, *9th edition*. Brooks Cole.

## Reference Books

1. Kreyszig E (2011). Advanced Engineering Mathematics, *10th edition*. Wiley.
2. Jeffrey A (2001). Advanced Engineering Mathematics. Academic Press.

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MATH208: MATHEMATICAL ANALYSIS
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Credit 3
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## Introduction

The study of mathematical analysis is indispensable for prospective students in different sectors of graduate level, specially, in science, engineering, economics and management sciences. This course contains basic properties of real numbers, sets, intervals; sequences and series of real numbers; different properties of limits, continuity, differentiability and integration of a function; and basic concepts of measure theory and probability measure. Calculus is one of most fundamental courses in mathematical sciences and this is the prerequisite course for mathematical analysis.

## Objectives

The course has great value for a student who wishes to go beyond the routine techniques to solve standard problems, and who wants to extend ideas to a new context. It develops the ability to analyze mathematical situations properly and precisely. It also helps the students to learn how to work comfortably with concepts that initially seemed so mysterious.

## Learning Outcomes

Upon completion of the course, students are expected to (i) develop the ability to analyze mathematical situations properly and precisely, (ii) learn to work comfortably with concepts that initially seemed so mysterious, (iii) know real numbers, sets, intervals; sequences and series of real numbers and their convergence and divergence; Metric space and topological space and their properties; different properties of limits, continuity, differentiability and Riemann integral of a function; and basic concepts of measure theory and probability measure.

## Contents

The real number system; axioms and completeness and its consequences; Dedekind cut, sets, compact sets; simple operation on them.

Sequence of functions of one and several variables; limit; continuity; continuous functions; uniform continuity; differentiation and integration; infinite series of constants and functions; convergence and divergence; power series: differentiation and integration of power series; Taylor expansion with remainder or in infinite series.

Metric and topological spaces; limit points; open and closed sets; interior and exterior points; boundary points; continuous mapping and Cauchy sequences.

Measure and integrals on abstract sets on real lines; Cramer measurability: fundamental definitions; auxiliary lemma; fundamental theorems; measurable functions; Lebesgue measure on a real line, plane; integrals; Riemann-Steiljes integrals.

## Textbook

1. Rudin W (1976). Principles of Mathematical Analysis. McGraw-Hill.

## Reference Books

1. Pugh CC (2015). Real Mathematical Analysis. Springer.
2. Rudin W (2017). Principles of Mathematical Analysis, *3rd edition*. McGraw-Hill.

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AST230: R FOR DATA SCIENCE
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Credit 2
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## Introduction

Any scientific task without the knowledge of software is difficult to imagine and complete in the current scenario. R is a free software that is capable of handling mathematical and statistical manipulations. It has its own programming language as well as built-in functions to perform any specialized task. Students intend to learn the basics of R software in this course.

## Objectives

The objective of the course are to teach the basics of R programming language that includes understanding different types of R objects, writing functions, reading/writing data of different formats, basic programming tools, and creating different types of plots. In addition, Python, another data analytic software will be introduced.

## Learning Outcomes

After completion of the course students are expected to (i) be able to learn the basics of R programming language that includes understanding different types of R objects, (ii) writing functions, reading/writing data of different formats, basic programming tools, and (iii) creating different types of plots. Students will also be introduced with Python.

## Contents

Introduction to R: History and overview of R programming language, R objects, data structure (e.g. lists, data frames, etc.), reading and writing data files, subsetting R objects, vectorized operations, control structures, functions (both in-built and custom), simulation, and calling C function from R.

Exploratory data analysis with R: managing data with different tidyverse packages (e.g. dplyr, ggplot2, etc.), exploratory graphs (grammar of graphics), and generating summary statistics.

Application of R in optimizing non-linear functions using Newton-Raphson iterative procedure, numerical integration and differentiation.

## Textbooks

1. Wickham H and Golemund G (2017). R for Data Science: Import, Tidy, Transform, Visualize, and Model Data. O'Reilly.



## Reference Books

1. Wickham H (2019). *Advanced R, Second Edition*. Chapman & Hall/CRC.
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AST231: STATISTICAL SIMULATION

Credit 2

## Introduction

This course is designed to introduce computational methods and simulation techniques, which will be helpful for understanding theoretical concepts and practical applications of probability and sampling distributions, and statistical inference, including point and interval estimation and test of hypotheses.

## Objectives

The main objective of this course is to introduce students to the theory of simulation and illustrate to them the theoretical concepts of sampling distributions and statistical inference using computer-simulated data. The course also aims at introducing students to computational methods required for fitting probability distributions, conducting point and interval estimation, and performing test of hypotheses using real-life datasets.

## Learning Outcomes

Upon completion of this course, the students should be able to (i) acquire detailed theoretical knowledge of common techniques of simulating data, (ii) write computers codes for simulating data from different probability distributions and use these data to illustrate theoretical concepts related to sampling distributions and statistical inference and (iii) apply computational methods required for fitting probability distributions, conducting point and interval estimation, and performing test of hypothesis.

## Contents

Concepts of simulation and its uses in statistics; random number generations: congruential generators, seeding; random variate generations: inversion method (direct method), rejection method (indirect method); Monte-Carlo integration: hit-and-miss method, improved Monte-Carlo integration; variance reduction: antithetic sampling, importance sampling, control variates. Use of simulated, repeated sampling and real datasets for illustrating theoretical and practical aspects of fitting probability distributions, sampling distributions, point and interval estimation, and tests of hypotheses.

## Textbooks

1. Jones O, Maillardet R and Robinson A (2009). *Introduction to Scientific Programming and Simulation using R*. Chapman & Hall/CRC.

## Reference Books

1. Robinson EA (2011). *Probability Theory and Applications*. Springer.
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**Introduction**

Statistical computing is crucial in addressing real-life problems by utilizing statistical techniques and computational tools and providing a framework for understanding and making sense of the data. This computing course will discuss the applications of the statistical methods discussed in the courses design of experiment and demography.

**Objectives**

The course's main objective is to teach students to use statistical software (e.g., R) and analyze experimental design and demography data. The specific objective is to provide hands-on learning by incorporating practical exercises and real-world examples to equip students with the knowledge and skills needed to excel in conducting scientific research or working in industry.

**Learning Outcomes**

By the end of the course, students will (i) have a solid understanding of the use of statistical software, e.g., R, and methods to analyze data in the area of experimental design and demography, (ii) learn how to apply the models related to different experimental designs (CRD, RBD, BIBD) to analyze the data in the field of agriculture, industry, and medicine, (iii) learn to analyze and interpret demographic data, gaining insights into population trends, age-sex structures, fertility, mortality, migration, population projections and population growth rates, and (iv) be equipped with the skills to write programs to obtain statistical results from data in the relevant field and draw meaningful conclusions from statistical analyses, which are essential for informed decision-making in various fields for public policy and planning.

**Contents**

Problems related to design of experiments (completely randomized, randomized block, Latin square, split-plot and nested designs) and demography, calculation of different measures related to fertility and mortality, and lifetable.

Each student must be examined by a committee of selected members at the end of the academic year.

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### 3.3 DETAILED SYLLABUS - THIRD YEAR

AST301: DESIGN AND ANALYSIS OF EXPERIMENTS II

Credit 4

#### Introduction

This course deals with the concepts and techniques used in the factorial design. The course examines how to design factorial experiments, carry them out, and analyze the data. Experiments with random factors and nested and split designs are also discussed in this course.

#### Objectives

The main objectives of the course is to teach the basic ideas of factorial design; design the experiments involving up to 2 and 3 factors with  $k$  levels; analyze the data from such experiments; interpret the results of any analysis; and design and analyze the experiments involving random factors. Also to teach the methods involved to design and analysis the experiments involving  $k$  factors each with two levels and three levels.

#### Learning Outcomes

After completing the course, the students are expected to (i) design the experiments involving up to two and three factors with  $k$  levels, (ii) analyze the data from such experiments and interpret the results, (iii) understand the concept of blocking and confounding for the designs involving  $k$  factors with two levels, (iv) understand design and analysis the fractional factorial experiments for  $k$  factors each with two levels and the experiments involving random factors.

#### Contents

Introduction to factorial designs: basic definition and principles; advantage of factorials; two-factor factorial design; statistical analysis of fixed effects model, model adequacy checking, estimating model parameters, choice of sample size, assumption of no interaction in a two-factor model, one observation per cell; general factorial design; fitting response curve and surfaces; blocking in a factorial design.

$2^k$  factorial design: introduction;  $2^2$  design;  $2^3$  design; general  $2^k$  design; a single replicate in  $2^k$  factorial design; blocking in a  $2^k$  factorial design; confounding in  $2^k$  factorial design; confounding in  $2^k$  factorial design in two blocks; confounding in  $2^k$  factorial design in four blocks; confounding in  $2^k$  factorial design in  $2^p$  blocks; partial confounding.

Two-level fractional factorial designs: one-half fraction of  $2^k$  design; one-quarter fraction of  $2^k$  design; general  $2^{k-p}$  fractional factorial design; resolution III designs; resolution IV and V designs.

Three-level and mixed-level factorial and fractional factorial designs:  $3^k$  factorial design, confounding in  $3^k$  factorial design, fractional replication of  $3^k$  factorial design, factorials with mixed levels.

Response surface methods: introduction to response surface methodology; method of steepest ascent; analysis of second-order response surface; experimental designs for fitting response surfaces; mixture experiments; robust designs.

Experiments with random factors: random effects model; two-factor factorial with random

factors; two-factor mixed model; sample size determination with random effects; rules for expected mean squares; approximate F tests; approximate confidence intervals on variance components; modified large-sample method; maximum likelihood estimation of variance components.

Nested and split-plot designs: two-stage nested designs; statistical analysis, diagnostic checking, variance components; general  $m$ -staged nested design; designs with both nested and factorial factors; split-plot design; split-plot designs with more than two factors; split-split-plot design, strip-split-plot design.

### Textbooks

1. Montgomery DC (2019). Design and Analysis of Experiments, *10th edition*. Wiley.

### Reference Books

1. Dean AM, Voss AM, and Draguljić (2017). Design and Analysis of Experiments, *2nd edition*. Springer.
2. Bailey R (2008). Design of Comparative Experiments. Cambridge.

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AST302: SAMPLING METHODS II
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Credit 3
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### Introduction

This course introduces advanced sampling methods used in sample survey. It covers sampling of unequal clusters, two-stage sampling, multistage sampling, methods for estimating variance in complex surveys, and non-sampling errors.

### Objectives

To acquaint students with the methodologies associated with the advanced sampling techniques.

### Learning Outcomes

Upon completion of the course, students will be able to (i) understand the necessity of multi-stage sampling (ii) formulate the multi-stage design (iii) know the methods for estimating variance in complex multi-stage design, and (iv) implement methods for designing a survey, particularly national level large scale survey.

### Contents

Probability proportional to size (PPS) sampling: motivating examples, with replacement (WR) sampling: cumulative measure of size method and Lahiri's method, Hansen-Hurwitz (H-H) estimator (unbiasedness, variances, estimated variance), comparison with SRS, optimum measure of size, PPS without replacement (WOR) sampling: challenges and solutions, initial probabilities, normalizing probabilities, inclusion probabilities and their relation with the sample size, Horvitz-Thompson (H-T) estimator (unbiasedness, variance, estimated variance), different methods of PPSWOR: Brewer's method, Durbin's method, Des Raj method,

Murthy's method, Rao- Hartley-Cochran method, Multinomial distribution for PPSWR sampling, H-T estimator in case of PPSWR sampling.

Sub-sampling, sub-sampling of unequal sized clusters: different estimators and their variances, two-stage sampling: design, estimators (total, mean), variances and their unbiased estimators, three stage sampling: design, estimators (total, mean), variances and their estimators, general framework (two-stage and three-stage) for estimating population total, different sampling designs at different stages, determination of sample sizes in two and three-stage sampling, optimum sampling and sub-sampling fractions, use of information from pilot survey.

Concept of double sampling and its necessity, application in stratified sampling, and in Ratio and Regression estimators, repeated sampling from the same population: sampling on two and more than two occasions.

Complex survey: definition and challenges involved in complex surveys, approaches of variance estimation (VE), replication methods for VE: random group method, balanced repeated replication (balanced half-sample replication) method, Jackknife method and Bootstrap method, implementation of replication methods in complex sampling designs, post-stratification.

Non-sampling errors: sources of the errors, effects of nonresponse, inference on population proportion in presence of nonresponse, types of nonresponse, Call-backs and its effects, Hansen and Hurwitz approach for nonresponse, Politz-Simmons adjustment for bias reduction, mathematical model for errors of measurement, mechanism of nonresponse, imputation and its different techniques.

Special sampling designs: multiplicity, network sampling: design and estimation (multiplicity and Horvitz-Thompson estimators for population total, and their different properties), adaptive sampling: adaptive cluster sampling (ACS) and related concepts used in ACS, Hansen-Hurwitz and Horvitz-Thompson estimators for population total, and their different properties.

### **Textbooks**

1. Cochran WG (1977). Sampling Techniques, *3rd edition*. Wiley.

### **Reference Books**

1. Lohr SL (1998). Sampling: Design and Analysis. Duxbury.
2. Thompson SK (2012). Sampling, *3rd edition*. Wiley.
3. Kirk MW (2007). Introduction to Variance Estimation, *2nd edition*.Wiley.

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AST303: LINEAR REGRESSION ANALYSIS

Credit 4

### **Introduction**

This introductory course gives an overview of regression types and details the application of multiple linear regression. This course covers the theory behind regression analysis, multiple linear regression, classical estimation and testing methods, and residual analysis. It also covers the formulation, interpretation and validation of linear regression models, and hands on use of a statistical package to see how the theory can be applied to answer a specific research question.

## Objectives

The main objectives of the course to acquaint students with Least Square methods and concept of linear regression, correlation, and its applications. To approach the material with matrices algebra. To develop the ability to build regression models. To acquaint students with transformations, qualitative variable in the model which broaden the use of linear regression theory. To gain familiarity with the use of modern statistical software packages for building a statistical model.

## Learning Outcomes

Upon completion of the course, students are expected to know (i) the concept of linear regression and correlation, (ii) about model formulation and fitting the model using least squares method, (iii) interpret the results, (iv) model diagnosis, (v) how to identify the best regression model, and vi) regression with qualitative variable in the model.

## Contents

Measures of association for quantitative data: correlation and inference concerning correlation; regression and model building, motivating examples, uses of regression.

Simple linear regression model: model for  $E(Y|x)$ , least squares estimation, assumptions related to errors, maximum likelihood estimation (MLE) of model, sampling distribution of MLEs of the model parameters, inferences concerning the model parameters (confidence intervals and t-test), confidence interval estimate of the  $E(Y|x)$  (confidence band).

Model accuracy and diagnostics: goodness of fit test ( $F$ -test, coefficient of determination,  $R^2$ ); prediction and prediction interval for a new  $Y$  at specific  $x$ , residual analysis: definition, normal probability plot, plots of residuals versus fitted values, residuals versus  $x$ , other residual plots, statistical tests on residuals; detection and treatment of outliers; concept of lack of fit and pure error, test for lack of fit, transformations as solution to problems with the model, weighted least squares.

Matrix representation of simple linear regression model, inference and prediction.

Multiple linear regression models: formulation of multiple regression models, estimation of the model parameters: least squares estimation, maximum likelihood estimation, sampling distributions of the MLEs, confidence interval and hypothesis testing for concerning model parameters; model accuracy and diagnostics: goodness of fit test ( $F$  test,  $R^2$ , adjusted  $R^2$ ), prediction of a new observation; extra sum of squares principles and its application in testing general linear hypothesis, checking all assumptions concerning model and use of remedy measures when assumptions are not valid, detection and treatment of outliers, influential observations.

Polynomial regression model: introduction; polynomial models in one variable: basic principles, piecewise polynomial fitting; polynomial models in two or more variables; orthogonal polynomials.

Indicator variables: the general concept of an indicator variable, use of the indicator variables in linear regression, models with only indicator variables, idea of regression models with an indicator response variable.

Variable selection and model building: the model building problem, consequences of model mis-specification, criteria for evaluating subset regression models, computational techniques

for variable selection.

Validation of regression models: concept, cross validation.

### **Textbooks**

1. Weisberg S (2013). Applied Linear Regression, *4th edition*. Wiley.

### **Reference Books**

1. Montgomery DC, Peck EA, and Vining GG (2012). Introduction to Linear Regression Analysis, *5th edition*. Wiley and Sons.
2. Draper NR and Smith H (1999). Applied Regression Analysis, *3rd edition*. Wiley.

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AST304: EPIDEMIOLOGY
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Credit 3
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### **Introduction**

This course covers the basic principles and methods of epidemiology, with an emphasis on critical thinking, analytic skills, and application to clinical practice and research. Topics include outcome measures, methods of adjustment, surveillance, quantitative study designs, and sources of data, analysis of exposure-disease relationship and causal inference. The course will provide tools for critically evaluating the literature and skills to practice evidence-based medicine.

### **Objectives**

The objective of the course is make students familiar with epidemiologic terminology, outcome measures, and study designs; to appreciate application of epidemiologic methods in the studies of both infectious and chronic diseases and current public health issues.

### **Learning Outcomes**

Upon completion of the course, students should (i) familiar with epidemiologic terminology, outcome measures, and study designs, (ii) familiar with the methods for estimating association measures such as incidence and prevalence rate, risk ratio, odds ratio etc., (iii) appreciate application of epidemiologic methods in the studies of both infectious and chronic diseases and current public health issues.

### **Contents**

Introduction: disease processes, statistical approaches to epidemiological data, study design, binary outcome data, causality.

Measures of disease occurrence: prevalence and incidence, disease rates, hazard function; review of simple random samples, probability, conditional probabilities, and independence of two events.

Measures of disease-exposure association: relative risk, odds ratio, relative hazard, risk, attributable risk.

Study designs: population-based studies, cohort studies, case-control studies, case-cohort studies; Assessing significance of  $2 \times 2$  tables obtained from cohort designs, case-control designs.

Estimation and inference for measures of association: odds ratio, sampling distribution and confidence interval for odds ratio, relative risk, excess risk, attributable risk.

Confounding and interaction: causal inference, counterfactuals, confounding variables, control of confounding variables by stratification, causal graphs, controlling confounding in causal graphs; Cochran-Mantel-Haenszel test, summary estimates and confidence intervals for odds ratio and relative risk after adjusting for confounding factors.

Interaction: multiplicative and additive interaction, interaction and counterfactuals, test of consistency of association across strata, overall test of association, a test for trend in risk.

Introduction to matching, types of matching, and analysis of matched studies.

### **Textbooks**

1. Jewell NP (2003). *Statistics for Epidemiology*. Chapman and Hall.

### **Reference Books**

1. Timothy L. Lash, Tyler J. Vander Weele, Sebastien Haneuse, and Kenneth J. Rothman (2021). *Modern Epidemiology, 4th edition*. Wolters Kluwer.
2. Fleiss JL, Levin B, and Paik MC (2003). *Statistical Methods for Rates and Proportions, 3rd Edition*. Wiley.

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AST305: LIFETIME DATA ANALYSIS I

Credit 3

### **Introduction**

This course deals with the analysis of survival or failure time data, which are commonly encountered in scientific investigations. It is being extensively used in medicine, clinical trials, biological and epidemiological studies, engineering, economics, and social sciences. This course provides an opportunity for students to learn lifetime probability distributions that are useful for modeling time-to-event data. Topics include lifetime distributions and non-parametric and parametric approaches for analyzing time-to-event data.

### **Objectives**

The course's primary focus is to make students familiar with the situation where censored data appear and to be able to analyze such data by implementing appropriate methods and models. Secondly, to introduce statistical theory and methodology for analyzing lifetime data obtained from censored samples, emphasizing statistical lifetime distributions, types of censoring, graphical techniques, and non-parametric/parametric estimation.

### **Learning Outcomes**

After successful completion of the course, students are expected to (i) understand the basic features of censored lifetime data, survival function, and hazard functions, (ii) distributions of



lifetime data, and (iii) both parametric and non-parametric estimation of survival and hazard functions.

## Contents

Basic concepts and models: lifetime distributions - continuous models, discrete models, a general formulation; some important models - exponential, Weibull, log-normal, log-logistic, gamma distributions, log-location-scale models, inverse Gaussian distributions, mixture models; regression models. Observation schemes, censoring, and likelihood: right censoring and maximum likelihood; other types of incomplete data; truncation and selection effects; information and design issues. Nonparametric and graphical procedures: nonparametric estimation of survivor function and quantiles; descriptive and diagnostic plots; estimation of hazard or density functions; methods of truncated and interval censored data; life tables. Inference procedures for parametric models: inference procedures for exponential distributions; gamma distributions; inverse Gaussian distributions; grouped, interval censored, or truncated data; mixture models; threshold parameters; prediction intervals.

Inference procedure for log-location-scale distributions: inference for location-scale distributions; Weibull and extreme-value distributions; log-normal and log-logistic distributions; comparison of distributions; models with additional shape parameters; planning experiment for life tests.

## Textbooks

1. Lawless J (2003). *Statistical Models and Methods for Lifetime Data, 2nd Edition*. Wiley.

## Reference Books

1. Kalbfleisch J and Prentice R (2003). *The Statistical Analysis of Failure Time Data, 2nd edition*. Wiley.
2. Collett D (2014). *Modelling Survival Data in Medical Research, 3rd edition*. Chapman & Hall/CR.

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AST306: STATISTICAL INFERENCE II

Credit 3

## Introduction

A branch of statistics has been developed to draw conclusion in a short time and cost-effective way regarding the population of interest which is ubiquitously known as statistical inference. It facilitates both parametric and nonparametric approaches under the umbrella of classical and Bayesian paradigms.

## Objectives

The course is designed to teach students on advanced methods of statistical inferences including, optimize techniques, parametric and semi-parametric inferential procedures, numerical methods, resampling techniques. Keeping the diversity of demands in current world, this course is designed in such a way that the students can build up their research career in a

wide variety of fields such as social science, medical statistics, clinical trials, spatial statistics, multivariate statistics, etc.

### **Learning Outcomes**

After completion of this course, students (i) will be able to draw statistical inference both in classical and Bayesian framework, (ii) will have ample skills in handling data to meet the inferential needs in diverse areas of applications.

### **Contents**

Statistical inference: parametric, nonparametric, and semiparametric inference.

Approximate and computationally intensive methods for statistical inference: the general problem of inference; likelihood functions; maximum likelihood estimation; optimization techniques-Newton type methods; EM algorithm-simple form, properties, uses in analyzing missing data, fitting mixture models and latent variable model; restricted maximum likelihood (REML) method of estimation; Multi-stage maximization; Efficient maximization via profile likelihood; confidence interval and testing hypothesis in these complex cases.

Bayesian method of inference: prior and posterior distribution, different types of prior, credible intervals and testing hypothesis; analytical approximations - asymptotic theory, Laplace approximation; numerical integral methods - Newton-Cotes type methods; Monte-carlo methods; simulation methods - Markov chain Monte Carlo.

Exact tests: test for single proportion and comparison of two proportions.

Resampling techniques: bootstrap-confidence intervals, test, parametric bootstrap, advantages and disadvantages of parametric bootstrap; jackknife-confidence interval, test, and permutation test.

Nonparametric inference and robustness: introduction, inference concerning cumulative distribution function (cdf), quantiles and statistical functionals: empirical cdf, quantiles, estimating statistical functionals, influence functions, testing statistical hypothesis-one sample settings, two or more sample settings; tolerance limit; empirical density estimation- histograms, kernel, kernel density estimation.

### **Textbooks**

1. Mukhopadhyay N (2020). Probability and Statistical Inference. CRC Press.

### **Reference Books**

1. Rice J (2013). Mathematical Statistics and Data Analysis., *3rd Edition*. Cengage Learning.
2. Hogg RV, McKean J and Craig AT (2019). Introduction to Mathematical Statistics, *8th Edition*. Pearson.

**Introduction**

The objective of the course is to introduce several useful multivariate techniques, and making strong use of illustrative examples.

**Objectives**

The objective of the course is to teach students on the basic concept of analyzing multivariate data, the methods for summarizing the multivariate data, multivariate normal distributions, multivariate tests and the regression.

**Learning Outcomes**

On a general level the students should be able to understand the concept of analysing multivariate data. They should be familiar with a basic minimum level of matrix competency and with general aspects of handling multivariate data. On successful completion of the course the student will (i) appreciate the range of multivariate techniques available, (ii) be able to summarize and interpret multivariate data, (iii) have an understanding of the link between multivariate techniques and corresponding univariate techniques, (iv) be able to use multivariate techniques appropriately, undertake multivariate hypothesis tests, and draw appropriate conclusions.

**Contents**

Preliminaries of multivariate analysis: applications of multivariate techniques; the organization of data; data display and pictorial representations; distance.

Random vectors and random sampling: some basics of matrix and vector algebra; positive definite matrices; a square-root matrix; random vectors and matrices; mean vectors and covariance matrices; matrix inequalities and maximization; the geometry of the sample; random sample and expected values of sample means and covariance matrix; generalized variance; sample mean, covariance, and correlation as matrix operations; sample values of linear combinations of variables.

The multivariate normal distribution: the multivariate normal density and its properties; sampling from a multivariate normal distribution and maximum likelihood estimation; sampling distribution and large sample behavior of sample mean vector and sample variance-covariance matrix; assessing the assumption of normality; detecting outliers and data cleaning; transformation to near normality.

Inferences about a mean vector: the plausibility of mean vector as a value for a normal population mean; Hotelling  $T^2$  and likelihood ratio tests; confidence regions and simultaneous comparisons of component means; large sample inference about a population mean vector; inferences about mean vectors when some observations are missing; time dependence in multivariate data.

Comparisons of several multivariate means: paired comparisons and a repeated measures design; comparing mean vectors from two populations; comparison of several multivariate population means (one-way MANOVA); simultaneous confidence intervals for treatment effects; two-way multivariate analysis of variance; profiles analysis; repeated measures designs and growth curves.

Multivariate linear regression models: the classical linear regression model; least squares estimation; inferences about regression model; inferences from the estimated regression function; model checking; multivariate multiple regression; comparing two formulations of the regression model; multiple regression model with time dependent errors.

### **Textbooks**

1. Johnson RA and Wichern DW (2008). Applied Multivariate Statistical Analysis, *6th edition*. Prentice-Hall.

### **Reference Books**

1. Srivastava MS (2002). Methods of Multivariate Statistics. Wiley.
2. Anderson TW (2003). An Introduction to Multivariate Statistical Analysis. *3rd edition*. Wiley.

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AST308: RESEARCH METHODOLOGY
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Credit 3
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### **Introduction**

The research methodology course is fundamental to teaching students the theoretical and practical skills required to conduct research in various fields. The course introduces students to the fundamental principles of research design, data collection, data analysis, and report writing. It will cover a range of research approaches, including quantitative, qualitative, and mixed methods.

### **Objectives**

The course aims to provide students with hands-on experience in designing and conducting research studies, particularly to develop students' knowledge and understanding of how to formulate research questions, develop hypotheses, choose appropriate research methods, and collect and analyze data and write a report for scientific publication. In addition, the course is designed to provide students with the knowledge and skills necessary to conduct valid, reliable, and ethical research.

### **Learning Outcomes**

By the end of the course, students will learn how to formulate research questions, develop hypotheses, choose appropriate research methods, and collect and analyze data. Students will also learn about the various data collection techniques, such as surveys, interviews, observations, and statistical techniques for analyzing data. In addition to the theoretical components of the course, students will apply their knowledge through practical exercises and projects. Students should become competent in planning, conducting, evaluating, and presenting a research project.

### **Contents**

Foundations of Research: Meaning, concept, motivation, and objectives of the research; Types of research – descriptive vs. analytical, applied vs. fundamental, quantitative vs. qualitative,

conceptual vs. empirical, concept of the applied and basic research process. Criteria and steps of good research.

Language of research: Variables and attributes; concepts and constructs; theory and models; proposition and hypotheses: relational terminologies: independent and dependent variables, intervening variables, extraneous variables, moderating variables confounder variables.

Problem Identification and Formulation: Defining and formulating the research problem, the importance of literature review in defining a problem, identifying gap areas from literature and research database, research question, and formulation of research hypothesis.

Research Design and Methods: Research methods vs. methodology; features of a good research design, concept, types, and uses of exploratory, descriptive, and experimental research designs. Qualitative and quantitative research approach, mixed methods design. Concept of measurement, problems in measurement in research - validity, and reliability. Sampling: use of sampling techniques in research design; brief review of sampling and sample size determination.

Techniques of data collection: Qualitative approaches – focus group discussion (FGD), in-depth interview (IDI), key informant interview (KII) and their guidelines and checklist; concepts of ethnography, content analysis, and discourse analysis, Quantitative approach – the concept of a survey, mode of a survey – face-to-face interview, telephone interview, online/email, etc. Survey tools – Questionnaire, schedule, structured, semi-structured, open-ended, and close-ended questions. Data collection apps: survey CTO, Kobo Toolbox, etc.; Field Implementation – a pilot study, monitoring the data collection, quality control, and data validity.

Monitoring and Evaluation (M&E): Concept of monitoring and evaluation, objectives of M&E; performance monitoring versus performance evaluation. Key steps of M&E; M&E design: Baseline, ongoing, and end-line evaluation; evaluation criteria–relevance, effectiveness, efficiency, impact, and sustainability.

Human resources and budget in research: allocation of human resources, preparing a budget for research work.

Data Analysis: Steps of data preparation and analysis; Guidelines for using secondary data for research: when, how, and why;

Dissemination of Research findings: Different Steps in Writing Report, Layout of the Research Report; Effective presentation, preparing articles for peer review.

Research Ethics and Scholarly Publishing: Ethics-ethical issues, ethical committees (human and animal); IPR- intellectual property rights and patent law, commercialization, copyright, royalty; scholarly publishing concept and research paper design, citation, acknowledgment, plagiarism, reproducibility, and accountability.

Experiential Learning Project: Group project and field work – writing a research proposal, developing and implementing field data collection, data analysis, and report writing and presentation.

## **Textbooks**

1. Kothari CR and Garg G (2019). Research Methodology: Methods & Techniques. New Age.

## Reference Books

1. Gertler PJ, Martinez S, Premand P, Rawlings LB and Vermeersch CMJ (2017) . Impact Evaluation in Practice, *2nd edition*. World Bank Group, Washington DC.
2. Coninck JD, Chaturvedi K, Haagsma B, Griffioen H and Glas MVD (2008). Planning, monitoring and evaluation in development organizations: sharing training and facilitation experiences. Sage.

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AST330: STATA FOR DATA SCIENCE
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Credit 2
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## Introduction

This is an introductory course of the three popular statistical packages. Students will learn to implement different statistical techniques using these packages.

## Objectives

The course aims to develop computing skills of the students. The in-depth knowledge of the course will enable a student to analyse data from various sources.

## Learning Outcomes

A student is expected to (i) achieve basic skills on Stata/SPSS codes, (ii) learn how to analyse data coming from a survey/experimental study, (iii) be able to manage primary/secondary data to answer a specific query, (iv) learn implementation of a wide range of statistical techniques using SPSS and Stata.

## Contents

Introduction to Stata: different windows and files, help file and searching for information; data entry, reading both stata and other format of data file, combining Stata files; exploring data: example commands-browse, edit, list, sort, describe, assert, codebook; data management: creating a new data set specifying subsets of data with in and if qualifiers, generating and replacing variables, using functions based on egen command, converting numeric and string formats, creating new categorical and ordinal variables, reshaping or collapsing data, weighting observations, creating random data and random samples; graphs: example commands- histograms, scatterplots, line plots, connected-line plots, two-way plots, box plots, combining graphs; exploratory data analysis: summary statistics and tables: example commands - summarize, tabstat, table; frequency tables and two-way cross tabulations, multiple tables and multi-way cross tabulations, tables of means, medians and other summary statistics.

## Textbooks

1. Hamilton LC (2006). Statistics with Stata, Thomson Brooks/Cole.

## Reference Books

1. Acock AC (2010). A Gentle Introduction to Stata, *6th edition*. Stata Press.

## Introduction

Python has become one of the most popular programming languages for data science due to its simplicity, versatility, and robust data analysis and machine learning capabilities. As organizations continue to digitize and generate increasingly large amounts of data, open-source tools like Python can enable data manipulation and exploration, machine learning, and statistical analysis in a scalable manner. This course provides a gentle introduction to programming in Python and its applications in data science and analytics.

## Objectives

This course aims to give the students a working knowledge of Python programming. Students will learn programming fundamentals, basic data structures, writing functions, importing and exporting data of different formats, data manipulation, and data visualization using Python. This course will also prepare students for more advanced courses in data science and machine learning.

## Learning Outcomes

At the end of this course, students are expected to (i) understand the fundamentals of Python programming, (ii) produce insights from data through exploratory data analysis, and (iii) create effective data visualizations using Python.

## Contents

Fundamentals of Python: Installing Python and Jupyter Notebook; the basic syntax of a Python program, Python data types; expressions and variables; lists, tuples, sets, and dictionaries; writing conditions, loops, and functions.

Data analysis with NumPy and pandas: installing NumPy and pandas, NumPy arrays; indexing, slicing, and iterating NumPy arrays; arithmetic and matrix operations with NumPy; pandas objects– DataFrame, Series, and Index; data indexing and selection; handling missing data; combining and joining datasets, aggregation and grouping, exploratory data analysis.

Data visualization with matplotlib and seaborn: Bar plots, histograms, density plots. boxplots and scatterplots.

## Textbooks

1. McKinney W. (2022). Python for data analysis: Data wrangling with Pandas, NumPy, and Jupyter, *3rd edition*. O’Reilly.
2. VanderPlas J. (2016). Python data science handbook: Essential tools for working with data. O’Reilly.

## Reference Books

1. Grus, J. (2019). Data science from scratch: First principles with python. O’Reilly.

**Introduction**

This statistical computing course provides a comprehensive understanding of applications of the methods covered in the courses design and analysis of experiments, epidemiology, and lifetime data analysis to real-life problems, equipping students with the tools and knowledge to address real-life problems across various fields. By achieving these skills, students are expected to make data-driven decisions and contribute to solving the complex challenges faced by society today.

**Objectives**

This course aims to equip students with the skill to use statistical software (e.g., R, Stata, or Python) to apply the methods discussed in the courses design and analysis of experiments, epidemiology, and lifetime data analysis. By achieving these skills, students are expected to tackle problem-solving challenges while working in industry, agency, or academia, make data-driven decisions, and contribute to planning and policy.

**Learning Outcomes**

Upon completion of the course, students should (i) understand how to use R or Stata to fit linear models used in factorial experiments, (ii) able to perform bivariate analysis of epidemiological studies, and (iii) able to obtain non-parametric and parametric estimates of survival and cumulative hazards functions; (iv) able to interpret the statistical results for decision-making processes related to healthcare, engineering, finance, and more.

**Contents**

Analysis of factorial designs, screening experiments, split-plot designs, and response surfaces. Estimating odds ratio, risk ratio, and risk difference for different types of study designs and corresponding inference. Estimating the survival function and cumulative hazards function using non-parametric and parametric methods.

**Introduction**

This computing course is based on applications of regression models, multivariate methods, and statistical inference to real-life problems. By mastering these techniques for solving real-life problems, students will be equipped to analyze complex datasets, uncover meaningful insights, and contribute to data-driven decision-making processes in academia, industry, and research.

**Objectives**

The objectives of this computing course are to teach students the applications of some statistical methods (regression models, multivariate methods, and statistical inference) using statistical software (R, Python, and Stata) and interpret the results. More specifically, the idea is to engage students in hands-on exercises and projects that involve real-life datasets,



providing practical experience in applying regression models, multivariate methods, and statistical inference techniques to address real-world problems.

### **Learning Outcomes**

On successful completion of this course, the students are expected to: (i) understand the applications of linear regression models, (ii) able to make inference about mean vector and apply multivariate linear regression models to real-life problems, and (iii) perform parametric and nonparametric hypothesis tests and corresponding confidence intervals, (iv) effectively utilize statistical computing tools and software packages such as R, Stata, or Python to implement regression models, multivariate methods, and statistical inference techniques, (v) to manipulate and analyze large datasets, visualize results, and present their findings clearly and concisely.

### **Contents**

Problems related to fitting simple and multiple linear regression models, related inference, model diagnostics, and model selection; Exploratory analysis of multivariate data, multivariate tests, MANOVA and multivariate regression, hypothesis tests, confidence intervals, and bootstrap methods, and nonparametric tests.

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AST340: ORAL III
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Credit 2
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Each student must be examined by a committee of selected members at the end of the academic year.

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## 3.4 DETAILED SYLLABUS - FOURTH YEAR

AST401: ADVANCED PROBABILITY AND STOCHASTIC PROCESSES

Credit 3

### Introduction

This module covers two important parts, one is advanced probability and another is stochastic processes. The module begins with a brief overview of modern probability and convergence of random variable and then moves on to the stochastic process to describe Markov chains, Poisson process, continuous time Markov chain and renewal process.

### Objectives

The course is designed to teach students on advanced probability theory including law-of-large number, convergence of a random variable and teach students Markov processes with discrete/continuous time-parameter and discrete/continuous state space, including branching processes, Poisson processes, birth and death processes, and Brownian motion.

### Learning Outcomes

Upon completion of the course the students are expected to (i) know how to apply advanced probability in real life problems and how to give prediction using transition probability and gamblers ruin theory, (ii) formulate simple stochastic process models in the time domain and provide qualitative and quantitative analyses of such models, (iii) understand the applications of stochastic processes in real life situations.

### Contents

Modern probability: events as sets, field, sigma field, probability measure, Borel field and extension of probability measure, measure theoretic approach of random variables; probability space.

Convergence of random variables: modes of convergence: almost sure,  $r$ th mean, in probability, in distribution, their interrelationship; law of large numbers, strong and weak laws of large numbers, limiting distribution; central limit theorem; law of iterated logarithm; martingale.

Markov chains: introduction, Chapman-Kolmogorov equations, classification of states, limiting probabilities, gambler's ruin problem, mean time spent in transient states, branching processes, time reversible Markov chains, Markov chain Monte Carlo methods, Markov decision processes, hidden Markov chains.

Poisson process: exponential distribution, properties, convolutions of exponential random variables; counting processes, Poisson process, interarrival and waiting time distributions, further properties of Poisson processes, generalizations of the Poisson process, nonhomogeneous Poisson process, compound Poisson process, conditional or mixed Poisson processes.

Continuous-time Markov chains: introduction, continuous-time Markov chains, birth and death processes, transition probability function, limiting probabilities, time reversibility.

Introduction to queueing theory: Classical M/M/1 queue, global and local balance, performance measures, Poisson arrivals see time averages (PASTA) property, M/M/1/S queueing systems, blocking probability, performance measures, multi-server systems – M/M/m, perfor-

mance measures, waiting time distribution of M/M/m, performance measures of M/M/m/m with finite customer population, Erlang loss systems.

Renewal theory and its applications : introduction, distribution of renewals, limit theorems and their applications, renewal reward processes, regenerative processes, semi-Markov processes, Markov renewal processes.

### Textbooks

1. Grimmett G and Stirzaker D (2001). Probability and Random Processes, *3rd edition*. Oxford.

### Reference Books

1. Ross S (2010). Introduction to Probability Models, *10th edition*. Elsevier.
2. Jones PW and Smith P (2018). Stochastic Processes: An Introduction, *3rd Edition*. Routledge.

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AST402: STATISTICAL MACHINE LEARNING

Credit 3

### Introduction

The course provides a broad but thorough introduction to the methods and practice of basic statistical machine learning and its core methods, models, and algorithms.

### Objectives

The aim of the course is to provide students of applied statistics and data science with detailed knowledge of how the basic Machine Learning methods work and how statistical models can be brought to bear in computer systems not only to analyze large, high-dimensional, and big data sets but also to let computers perform tasks, that traditional methods of computer science are unable to address.

### Learning Outcomes

After completing the course, students will have the knowledge and skills to (i) the concept of Artificial Intelligence, Big Data, and their areas. (ii) describe a number of models for supervised and unsupervised machine learning and regularized modeling techniques (iii) assess the strength and weaknesses of each of these models, (iv) know the underlying mathematical relationships within and across statistical learning algorithms, (v) develop and implement optimization methods for training of statistical models, (vi) design decision and optimal control problems to improve performance of statistical learning algorithms, (vii) design and implement various statistical machine learning algorithms in real-world applications, (viii) evaluate the performance of various statistical machine learning algorithms, (ix) demonstrate a working knowledge of dimension reduction techniques. (x) identify and implement advanced computational methods in machine learning.

## Contents

Artificial Intelligence and Big Data: Overview of basic concepts and techniques of Artificial Intelligence (AI), including its history and applications, and statistical machine learning. Data science concepts and their application areas. Overview of supervised and unsupervised learning.

Overview of Big Data, including its definition, sources, characteristics, and the challenges associated with processing and analyzing large datasets. Big data applications: examples and use cases. The Hadoop framework and its various components include HDFS, MapReduce, YARN, and Hive.

Statistical learning: Statistical learning and regression, the curse of dimensionality and parametric models, assessing model accuracy and bias-variance trade-off, classification problems, and K-nearest neighbors.

Linear regression: Model selection and qualitative predictors, interactions, and nonlinearity.

Classification: Introduction to classification, logistic regression, and maximum likelihood, multivariate logistic regression and confounding, case-control sampling and multiclass logistic regression, linear discriminant analysis and Bayes theorem, univariate linear discriminant analysis, multivariate linear discriminant analysis, and ROC curves, quadratic discriminant analysis and naive bayes.

Resampling methods: Estimating prediction error and validation set approach, k-fold cross-validation, cross-validation- the right and wrong ways, the bootstrap, more on the bootstrap. Linear model selection and regularization: Linear model selection and best subset selection, forward stepwise selection, backward stepwise selection, estimating test error using Mallows' Cp, AIC, BIC, adjusted R-squared, estimating test error using cross-validation.

Shrinkage methods: Ridge regression, Lasso, adaptive Lasso, Group Lasso, elastic net and adaptive elastic net, bridge, tuning parameter selection for ridge regression, lasso, and elastic net, total variation regularization.

Dimension reduction and unsupervised machine learning techniques: Techniques to reduce the dimension of data, principal components and principal components regression and partial least squares. Clustering (K-means, Fuzzy C-means, Hierarchical Clustering).

Introduction to Decision trees and Classification trees.

Statistical machine learning case studies in R.

## Textbooks

1. James G, Witten D, Hastie T and Tibshirani R (2013). An Introduction to Statistical Learning: with Applications in R. Springer.

## Reference Books

1. Hastie T, Tibshirani R and Friedman J (2009). The Elements of Statistical Learning: Data Mining, Inference and Prediction, *2nd edition*. Springer.
2. Russell S and Norvig, P (2020). Artificial Intelligence: A Modern Approach, *4th edition*. Pearson Education.

## Introduction

Multivariate analysis skills have been recognized as part of the key requisites for statistical analysts. The complexity of most phenomena in the real world requires an investigator to collect and analyze observations on many different variables instead of a single variable. The desire for statistical techniques to elicit information from multivariate dimensional data thus becomes essential and crucial for data analysts. This course focuses on multivariate methods based on normal theory. It gives students working knowledge on how to analyze data and solve problems involving measurements of  $p$  variables on each of  $n$  subjects.

## Objectives

The objective of this course is to give students experience with multivariate techniques in the analysis of research data. The aim is to teach students how to select appropriate methods of multivariate data analysis and interpret the results.

## Learning Outcomes

Having successfully completed this course, students should be able to (i) know the theoretical concept of advanced multivariate methods, (ii) know about data-dimension concept, necessity and techniques (iii) apply the methods for analysing real life problem and interpret the results.

## Contents

Principal components: population principal components, summarizing sample variations by principal components, graphing the principal components, large sample inference.

Factor analysis: the orthogonal factor models, methods of estimation (maximum likelihood estimates and principal factor analysis), selection of loadings and factor (factor rotation, varimax rotation, quartimax rotation, oblimin rotations), factor scores, structural equations models.

Canonical correlation analysis: canonical variates and canonical correlations, sample canonical variates and sample canonical correlations, large sample inference.

Discrimination and classification: separation and classification of two populations, classification of two multivariate normal populations, evaluating classification functions, Fisher's discriminant function, classification with several populations, Fisher's method for discriminating several populations.

Clustering: similarity measures, hierarchical clustering methods, nonhierarchical clustering methods; fuzzy clustering, determination of number of clusters: Gap statistics and its several modifications, several cluster validity indices, cluster's homogeneity test; multidimensional scaling.

## Textbooks

1. Johnson RA and Wichern DW (2008). Applied Multivariate Statistical Analysis, *6th edition*. Prentice-Hall.

## Reference Books

1. Srivastava MS (2002). *Methods of Multivariate Statistics*. Wiley.
2. Anderson TW (2003). *An Introduction to Multivariate Statistical Analysis. 3rd edition*. Wiley.

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AST404: ECONOMETRIC METHODS
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Credit 4
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## Introduction

This course covers a range of econometric methods required to conduct empirical economic research and understand applied econometric results. Topics include models for panel data, simultaneous equations models, models with lagged variables, and limited dependent variables.

## Objectives

To introduce students to the basic principles of econometric analysis. To gain theoretical understanding of the methods needed for econometric research including their underlying assumptions, advantages and limitations. To understand how to use different econometric tools in real-world economic problems and interpret findings.

## Learning Outcomes

On successful completion of this course the students should be able to (i) understand the basic principles of econometric analysis and econometric model building, (ii) gain theoretical understanding of the methods/models needed for econometric research including their underlying assumptions, advantages and limitations and (iii) understand how to use different econometric tools in real-world economic problems and interpret findings.

## Contents

Econometric modeling, data and methodology; specification analysis and model building: bias caused by omission of relevant variables, pretest estimation, inclusion of irrelevant variables, model building; testing non-nested hypotheses, encompassing model, comprehensive approach-J test, Cox test; model selection criteria.

Models for panel data: fixed effects: testing significance of group effects, within- and between-groups estimators, fixed time and group effects, unbalanced panels and fixed effects; random effects: GLS, FGLS, testing for random effects, Hausman's specification test.

Simultaneous equations models: illustrative systems of equations, endogeneity and causality; problem of identification: rank and order conditions for identification; limited information estimation methods: OLS, estimation by instrumental variables (IV), Two-Stage Least Squares (2SLS), GMM Estimation, limited information maximum likelihood and the k class of estimators, 2SLS in nonlinear models; system methods of estimation: Three-Stage Least Squares (3SLS). full-information maximum likelihood, GMM estimation, recursive systems and exactly identified equations; comparison of methods-Klein's Model I; specification tests; properties of dynamic models: dynamic models and their multipliers.

Models with lagged variables: lagged effects in a dynamic model, lag and difference operators;

simple distributed lag models: finite distributed lag models, infinite lag model: geometric lag model; Autoregressive Distributed Lag (ARDL) models: estimation of the ARDL model, computation of the lag weights in the ARDL model, stability of a dynamic equation, forecasting; Vector Autoregressions (VAR): model forms, estimation, testing procedures, exogeneity, testing for Granger causality, impulse response functions, structural VARs, application: policy analysis with a VAR.

Limited dependent variable: truncated distributions, moments of truncated distributions, truncated regression model; censored data: censored normal distribution, censored regression (Tobit) model, estimation, issues in specification; censoring and truncation in models for counts, application: censoring in the Tobit and Poisson regression models.

### **Textbooks**

1. Greene WH (2011). *Econometric Analysis, 7th edition*. Prentice Hall.

### **Reference Books**

1. Gujarati DN (2010). *Basic Econometrics, 5th edition*. McGraw-Hill.
2. Wooldridge JM (2010). *Introductory Econometrics: A Modern Approach, 5th edition*. Cengage Learning.

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AST405: LIFETIME DATA ANALYSIS II

Credit 3

### **Introduction**

This course deals with modeling survival or failure time data. Both parametric and semi-parametric approaches are discussed in the course. A brief introduction to competing risks and frailty models is also provided.

### **Objectives**

The course primarily focuses on familiarizing students with regression models commonly used to analyze time-to-event data. Both the accelerated failure time model and Cox's proportional hazards model will be discussed in detail. Students will learn about the methods for analyzing competing risk models and correlated time-to-event data.

### **Learning Outcomes**

After successful completion of the course, students are expected to (i) formulate a regression model for time-to-event data and interpret the model fits, (ii) be able to analyze competing risks and frailty model.

### **Contents**

Parametric regression models: log-location-scale (Accelerated Failure Time) regression models, proportional hazards regression models; graphical methods and model assessment; inference for log-location-scale models; extensions of log-location-scale models; hazard-based models.

Semiparametric multiplicative hazards regression models: methods for continuous multiplicative hazards models - estimation and tests for regression parameter vector, comparison between two or more lifetime distributions, justification, and properties of the likelihood function, adjustment of tied lifetimes, estimation of baseline cumulative hazard function, stratification, time-varying covariates, model checking.

Competing risks: introduction, hazard, and cumulative incidence function, modeling cause-specific hazards and cause-specific incidence.

Frailty models: introduction to frailty, gamma frailty distributions, parametric frailty model, semi-parametric frailty model, and shared frailty model.

### Textbooks

1. Lawless J (2003). Statistical Models and Methods for Lifetime Data, *2nd Edition*. Wiley.

### Reference Books

1. Kalbfleisch J and Prentice R (2003). The Statistical Analysis of Failure Time Data, *2nd edition*. Wiley.
2. Collett D (2014). Modelling Survival Data in Medical Research, *3rd edition*. Chapman & Hall/CR.
3. Therneau TM and Grambsch PM (2000). Modeling survival data: extending Cox model. Springer.

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AST 406: QUALITY CONTROL AND OPERATIONS RESEARCH
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Credit 4
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### Introduction

This course deals with the concepts and techniques used in the industry to maintain the quality of the process. Concepts of different types of control charts and their application in industry are discussed in this course. Basic concepts of acceptance sampling and how to design an acceptance sampling are also discussed. The concept and solution procedure of linear programming problem, duality and sensitivity analysis are discussed. Introduction of game theory, in particular the two person zero sum game are discussed.

### Objectives

The course is designed for the students to teach (i) the basic ideas of control chart techniques, (ii) to apply and interpret control charts for variables and attributes, (iii) design acceptance sampling plan, (iv) how to find optimal solution using linear programming problem.

### Learning Outcomes

On successful completion of this course, the student is expected to: (i) understand the basic ideas of control chart techniques; (ii) apply and interpret control charts for variables and attributes; (iii) design acceptance sampling plan; and (iv) find optimal solution using linear programming problem.



## Contents

### *Part A (Quality Control)*

Fundamental concepts of industrial statistics and its purposes; industrial quality control: total quality control; statistical quality control; chance and assignable causes of variation; statistical process control.

Control chart: concept of control chart; statistical basis of the control chart; basic principles; choice of control limits; sample size and sampling frequency; rational subgroups; analysis of patterns on control charts; sensitizing rules for control charts; necessary steps for constructing control charts; types of control charts (control charts with standard given and control charts with no standard given); control charts for attributes: concepts of nonconformity; non-conforming unit; defect; defective unit; p-chart; d-chart; c-chart; u-chart; basic concepts of control charts for variables; statistical basis and interpretation of  $\bar{X}$ , R and S charts.

Cumulative sum and exponentially weighted moving average control charts: the cumulative sum control chart; basic principles; the tabular or algorithmic cusum for monitoring the process mean; recommendations for cusum design; the standardized cusum; the exponentially weighted moving average control chart for monitoring the process mean; design of an EWMA control chart; robustness of the EWMA to non-normality; the moving average control chart.

Acceptance sampling: basic concepts of acceptance sampling; OC curve and its uses; types of OC curves; properties of OC curves. Single sampling plan: basic concepts of single sampling plan for attributes; construction of type A and type B OC curves under single sampling plan for attributes; specific points on the OC curve (AQL, LTPD); rectifying inspection; AOQ; AOQL; ATI; ASN; designing a single sampling plan; double sampling plan: basic concepts of double sampling plan; OC curve; ASN: AOQ; ATI; designing a double sampling plan; introduction to multiple sampling plan and sequential sampling analysis; acceptance sampling plan by variables: basic concepts of acceptance sampling plan; types of sampling plans; designing a variable sampling plan with a specified OC curve.

### *Part B (Operations Research)*

Nature and impact of OR approach; phases of OR; concept of linear programming problem (LPP); construction of LPP; solution of LPP: graphical and the simplex method; revised simplex method; big-M method, two phase method; concept of convergence, degeneracy and cycling; duality: dual primal relationship and formulation of dual problems; sensitivity analysis: introduction to sensitivity analysis; game theory: finite and infinite games; zero sum games; two person zero sum games; pay off matrix; maximum and minimum criterion of optimal solution of a game; dominance property; algebraic method for the solution of a game; equivalence of rectangular game matrix and linear programming; application in real life situation using MATLAB/Octave software.

*\*In addition to the compulsory question, students should answer at least 2 questions from each of the parts (A, B).*

## Textbooks

1. Montgomery DC (2004). Introduction to Statistical Quality Control. Wiley.
2. Hillier FS, Lieberman GJ, Nag B and Basu P (2001). Introduction to Operations Research, 9th edition. McGraw-Hill.

## Reference Books

1. Carter M and Price CC and Rabadi G (2017). Operations Research: A Practical Introduction. *2nd edition*. CRC Press.
2. Joglekar AM (2010). Industrial Statistics: Practical Methods and Guidance for Improved Performance. Wiley.

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AST407: TIME SERIES MODELLING
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Credit 3
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## Introduction

This is an introductory course of time series theory. The objective of this course is to equip students with various classical time series models, deriving their properties, inference methods and forecasting techniques for analyzing time series data. From computational point of view, it aims to demonstrate the theory with real datasets. Conclusions and proofs are given for some basic formulas and models; these enable the students to understand the principles of time series theory.

## Objectives

This course is designed to make student familiar with time series data and methods for analysing such data and to use them in forecasting.

## Learning Outcomes

On successful completion of this course, the students are expected to (i) identify the main components of the time series and apply a suitable exponential smoothing technique to forecast with a variety of time series models such as additive or multiplicative seasonal models by updating the components, (ii) formulate time series regression models for the series with trend and seasonal components and make forecasts from these models, (iii) Identify ARIMA models tentatively from ACF and PACF, (iv) estimate parameters of the ARIMA models by the method of moments, least squares method and maximum likelihood method, and (v) check the adequacy of the model and make forecasts.

## Contents

Introduction and examples of time series; simple descriptive techniques: time series plots, trend, seasonal effects, sample autocorrelation, correlogram, filtering.

Probability models: stochastic processes, stationarity, second-order stationarity, white noise model, random walks, moving average (MA) processes, autoregressive (AR) processes, ARMA processes, seasonal ARMA processes, the general linear process; properties, estimation and model building, diagnostic checking.

Forecasting: naive procedures, exponential smoothing, Holt-Winters, Box-Jenkins forecasting, linear prediction, forecasting from probability models.

Non-stationary time series: non-stationarity in variance-logarithmic and power transformations; non-stationarity in mean; deterministic trends; integrated time series; ARIMA and seasonal ARIMA models; modelling seasonality and trend with ARIMA models.

Stationary processes in the frequency domain: the spectral density function, the periodogram, spectral analysis.

Concept of state-space models: dynamic linear models and the Kalman filter.

### Textbooks

1. Jonathan DC and Kung-Sik C (2008). Time Series Analysis - With Applications in R. Springer.
2. Spyros M, Steven W and Rob H (1997). Forecasting – Methods and Applications, *3rd edition*. Wiley.

### Reference Books

1. Chatfield C (2003). The Analysis of Time Series, *6th edition*. Chapman & Hall.
2. Shumway RH and Stoffer DS (2011). Time Series Analysis and Its Applications: With R Examples. Springer.
3. Brockwell PJ and Davis RA (2002). Introduction to Time Series and Forecasting. *3rd edition*. Springer.

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AST408: GENERALIZED LINEAR MODELS

Credit 3

### Introduction

This course deals with different statistical models for the analysis of quantitative and qualitative data, of the types usually encountered in research.

### Objectives

To introduce to the students about the statistical methods including the general linear model for quantitative responses (including multiple regression, analysis of variance and analysis of covariance), binomial regression models for binary data (including logistic regression and probit models), and models for count data (including Poisson regression and negative binomial models). All of these techniques are covered as special cases of the Generalized Linear Model, which provides a central unifying statistical framework for the entire course.

### Learning Outcomes

After completing the course students will be familiar with (i) the exponential family of distributions, (ii) the class of generalized linear models (GLM) as regression models with responses from the exponential family of distributions, (iii) the concepts of link functions for modeling the correspondence between the expected value of the responses and covariates and of variance functions for specifying the correspondence between the expected values and variances of the responses, (iv) analyzing data from important special cases of GLMs, in particular logistic regression and Poisson regression, and (v) extensions of the GLM framework using quasi likelihood based on specified link and variance functions.

## Contents

Generalized linear models: exponential family of distributions; estimation: method of maximum likelihood, method of least squares, estimation of generalized linear models; inference: sampling distribution for scores, sampling distribution for maximum likelihood estimators, confidence intervals for model parameters, adequacy of a model, sampling distribution for log-likelihood statistic, log-likelihood ratio statistic (deviance), assessing goodness of fit, hypothesis testing; multiple regression: maximum likelihood estimation, log-likelihood ratio statistic.

Models for binary responses: probability distributions, generalized linear models, dose response models, general logistic regression, maximum likelihood estimation and log-likelihood ratio statistic, other criteria for goodness of fit, least square methods; multinomial distributions; nominal logistic regression models; ordinal logistic regression models.

Models for count data, Poisson regression and log-linear models: probability distributions, maximum likelihood estimation, hypothesis testing and goodness of fit.

## Textbooks

1. Dobson AJ and Barnett AG (2008). *An Introduction to Generalized Linear Models, 3rd edition*. Chapman & Hall.

## Reference Books

1. McCullagh P and Nelder JA (1989). *Generalized Linear Models, 2nd edition*. CRC Press.
2. Agresti A (2007). *An Introduction to Categorical Data Analysis, 2nd edition*. Wiley.
3. *Generalized Linear Models and Extensions, 4th edition*.

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AST409: OFFICIAL STATISTICS
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Credit 3
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## Introduction

Official statistics is a branch of statistics that deals with the collection, analysis, interpretation, and dissemination of data produced by government agencies and other official bodies. Its purpose is to provide accurate and reliable information on various aspects of society, such as the economy, population, health, education, and crime. Official statistics are used for various purposes, including policy-making, research, business-decision making etc.

## Objectives

The objective of the course is to introduce students to sources of official statistics and institutional, legal, and ethical aspects of official statistics and to introduce a methodological basis for measuring, processing, producing, and using official statistics for national policies and planning.

## Learning Outcomes

After completing this course, students are expected to (i) use statistical software (R, Python) to apply several multivariate and machine learning techniques to analyze real-life data, (ii) understand how to evaluate models generated from data, (iii) apply the algorithms to a real problem, optimize the models learned and report on the expected accuracy that can be achieved by applying the models. (iv) interpret the results and write for scientific publication.

## Contents

Domains of official statistics, concepts, definitions, and statistical standards; fundamental principles of official statistics; code of practice of official statistics in Bangladesh; Legal and ethical framework for official statistics; Sector-specific data quality assessment framework. Role of official statistics in monitoring the progress of global and national goals and policies. Data availability of the indicators of global and national goals and policies.

Use of administrative data in official statistics: sources of administrative data, collection, process, and use of administrative data in official statistics.

Use of survey data in official statistics; sources of surveys in Bangladesh; analysis of survey data for official statistics; use of survey weighting for official statistics.

Demographic Statistics: Population growth, techniques to measure it, doubling time concept in demography; population estimates and projections; different techniques of population projection- component method, arithmetic/linear method, geometric method, exponential method, matrix method, Lee-Carter model, Bayesian model etc., for population projections.

Health and well-being statistics: maternal and child health statistics, health services, general and chronic health statistics, health workforce.

Macro-Economy Statistics: GDP, GDP per capita, GDP growth, Inflation rate, Remittance etc. Business Economy Statistics: Short-and long-term business statistics; Science and technology; Environment and energy; Transport and travel; Labour Force Statistics: Income and social conditions; Employment, unemployment, and earnings.

Agricultural statistics: Food production and consumption (crop, forestry, and fisheries), Food Balance Sheet, Food insecurity experience scse (FIES), land use statistics, and climate and environmental statistics.

Education statistics: Enrollment, dropout, completion, transition rates at different levels of education, teacher student ratio.

National income: concepts and methods of measurement; social accounting matrix. Distribution of income and wealth: Pareto and Lognormal distribution.

Poverty: concept, steps in measurement. Defining poverty lines: subjective and objective poverty lines. Measures of poverty: headcount, gap, squared gap (Foster-Greer-Thorbecke), Sen, Sen-Shorrocks-Thon, Watts poverty indexes. Robustness of indexes: sampling error, measurement error. Poverty mapping, poverty comparisons. Vulnerability to poverty: measuring and quantifying vulnerability. The effect of taxation on inequality and poverty. Multidimensional poverty index.

Inequality: concept, measurement of positive and normative measures; Lorenz curve; Gini coefficient; Atkinson's index, Theil's index, Human development index. Inequality comparisons.

Psychometry: concept, measurement; intelligent and achievement tests; z-score and t-score; intelligent quotient.

Official statistics for all SDG indicators; Data visualization and GIS; time series of official statistics.

### Textbooks

1. Linneman TJ (2014). Social Statistics: Managing Data, Conducting Analyses, Presenting Results. Routledge.
2. Stillwell J and Clarke M (2011). Population Dynamics and Projection Methods, *4th edition*, Springer.
3. Haughton J and Khandker SR (2009). Handbook on Poverty and Inequality. Washington, DC: World Bank.

### Reference Books

1. Rahman PkMM (2016). Fundamentals of Social Statistics and Social Development. Osder.
2. Chadha NK (2009). Applied Psychometry. Sage.
3. NIPORT and ICF (2023). Bangladesh Demographic and Health Survey, 2022. Dhaka, Bangladesh and Rockville, Maryland, USA.

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AST430: STATISTICAL COMPUTING IV

Credit 2

### Introduction

This computing course is designed to teach students the applications of different multivariate techniques, methods in quality control and operations research, and machine learning techniques to solve real-life problems. By mastering these techniques, students will be able to extract meaningful insights and make data-driven decisions in various fields of research, policy-making, and planning.

### Objectives

The objective of this course is to provide hands-on experience in using statistical software such as R, Stata, or Python for applying different multivariate and machine learning techniques and methods in quality control and operation research so that students can equip them to tackle complex data analysis problems, optimize processes, and make informed decisions in fields such as business, manufacturing, healthcare, and logistics.

### Learning Outcomes

After completing this course, students are expected to (i) develop a strong foundation in multivariate techniques (PCA, factor analysis, discrimination analysis) and their applications, enabling them to analyze complex datasets, identify patterns, and extract meaningful insights for decision-making, (ii) gain the skills necessary to implement statistical process control techniques, optimize quality control processes, and ensure adherence to predefined quality

standards, (iii) learn how to formulate and solve mathematical models, optimize processes, and make data-driven decisions to improve operational efficiency and resource allocation, (iv) gain an understanding of key machine learning algorithms, including regression, classification, and clustering, and (v) learn how to train and evaluate models, perform feature selection, and apply machine learning techniques to real-life problems, ranging from image recognition to predictive analytics.

## Contents

Problems related to Inference and Multivariate analysis: principal component analysis, factor analysis, discriminant analysis, canonical correlation analysis, linear programming problem; Problems related to Machine Learning techniques: classification methods, resampling methods-different cross-validation and bootstrap, linear model selection procedures, regularized methods-lasso, elastic net, group lasso, and bridge, dimension reduction techniques, linear programming problems.

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AST431: STATISTICAL COMPUTING V
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Credit 2
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## Introduction

This statistical computing course focuses on real-life applications of the topics covered in the courses: time series analysis and econometrics methods. The course will equip students with the tools and techniques to analyze and interpret time series, and economic and financial data, make forecasts, estimate economic relationships, and contribute to economic research and policy analysis by integrating statistical software R, Stata, or Python.

## Objectives

The course's main objective is to familiarize the students with statistical software and packages (R, Stata, or Python) to apply time series and econometric methods for analyzing data and solving real-life problems. The aim is to prepare students with the skills and knowledge necessary to pursue careers in economics, finance, data analytics, or research institutions where time series analysis and econometrics are essential.

## Learning Outcomes

After completing this course, students are expected to (i) acquire proficiency in using statistical computing tools and software packages to implement time series analysis and econometric methods, (ii) simulate time series objects and explore its various features, (iii) fit different time series models to real-life data and identify the best models for forecasting by comparing different models based on AIC, BIC, and forecasting error, (iv) fit regression model for econometric data, and perform tests for multicollinearity, heteroscedasticity, autocorrelation, and also compare between compatible models, (v) fit dynamic regression models and simultaneous equation models to various real-life econometric data, (vi) gain a comprehensive understanding of time series and econometric models, and the skill to interpret and evaluate results and make informed decisions based on their analyses.

## Contents

Exploratory analysis of time series data, fitting time series models such as ARMA, ARIMA, etc. Fitting econometric models.

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AST432: STATISTICAL COMPUTING VI

Credit 2

### Introduction

This course deals with applying methods related to generalized linear models and lifetime data analysis to real-life data from diverse areas such as medicine, biological science, engineering, and social science. In addition, this course covers the use of statistical software and packages (e.g., R or Stata) of each model for computing results from real-life data. By combining computational tools with advanced statistical models, students will develop the skills to analyze complex data, model relationships, and draw meaningful conclusions in various domains.

### Objectives

This computing course's primary focus is to familiarize students with a broader range of models for different response variables, including binary, count, categorical, and time-to-event responses, and their applications to analyze real-life data in various fields such as healthcare, engineering, finance, and insurance. Secondly, to equip students with skills to implement statistical software and packages (e.g., R or Stata) to compute the results from real-life data and interpret them for meaningful conclusions.

### Learning Outcomes

Upon completion of the course, students will (i) develop a solid understanding of different kinds of models under GLMs, (ii) able to identify appropriate GLM formulations for different response variables and fit them using computational tools, and interpret the results in the context of the problem at hand, (iii) gain expertise in survival analysis techniques and models (both parametric and semiparametric models), applying them to analyze and interpret time-to-event data effectively, and (iv) achieve skills and knowledge necessary to contribute to advancements in healthcare, engineering, finance, and various other domains where statistical modeling and data analysis play a vital role.

## Contents

Exploratory analysis of categorical data, fitting glm: logistic regression models, binary logistic, multinomial logistic, ordinal logistic, log-linear models; Fitting survival models: AFT, Cox PH models, competing risks models, and frailty models.

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AST440: ORAL IV

Credit 2

Each student must be examined by a committee of selected members at the end of the academic year.

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Each student will be required to prepare a project report and present the report in a seminar. The project report is expected to reflect a student's ability to apply his or her knowledge of statistical methods in a novel research work, which could be applied or theoretical. For the project work, each student will be assigned to a supervisor (a faculty member of ISRT) at the beginning of the academic year. The project report submission and presentation should be made before the final examination. The 50% weight of the course will be allotted to project work, 10% for supervisor, and the remaining 40% for seminar presentation. The internal members of the examination committee will evaluate the performance in the seminars, and the report will be evaluated by two internal examiners nominated by the examination committee. A supervisor cannot evaluate the project report s/he has supervised.

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